

okay friends in continuation with earlier lecture one now graphical solution of system of linear in equation in two variables

so we have more than one linear equation in two variable and we have to solve that two or three in equation simultaneously

so for this solving simultaneous linear in equation means finding the set of points x y for which all the constants are satisfied here constants means linear equation in two variable in this simultaneous solution will be known as constants

so solution set may be an empty set for example for this in equation set of constants the solution will be empty set a bounded reason and an unbounded reason

so we will just discuss this example how to solve these in equations or these constants simultaneously

so to solve system of linear equation in two variable graphically first of all draw the graph of all the given linear inequalities we have already discussed how to draw the graph of linear inequalities in one variable or two variable then mark the feasible region of each lines means we have to mark solution region again we discuss how to find solution region find the common region which satisfy all the given linear inequalities then we have to find what will be the common region whether the given inequalities have common region may be common region may not have common region and this common region is required solution of given system of linear inequalities if the given system of linear inequalities have common region then that region may be bounded region may be unbounded region let us take another example solve system of linear inequalities graphically

$$3x + 2y \geq 24$$
$$3x + y \leq 15$$
$$x \geq 4$$

solution

so let this is first inequalities this is second and this is third inequalities so associated equation for one two and three are $3x + 2y = 24$ $3x + y = 15$ and $x = 4$

so these three are associated equation four given in equation

so for one $3x + 2y = 24$ put $y = 0$ implies $x = 8$ $x = 0$ implies $y = 12$

so points are $(8, 0)$ and $(0, 12)$ for second $3x + y = 15$ put $y = 0$ implies $x = 5$ $x = 0$ implies $y = 15$ and for third $x = 4$ is a line parallel to y axis passing through $(4, 0)$ now draw the graph of these three lines x y zero since we have to locate point $(8, 0)$ $(0, 12)$ and $(5, 0)$ and $(0, 15)$

so for sake of convenience we take one division equal to 2 4 6 8 10 12 14 16. 2 4 6 8 10 12 14 and this is 16 this is $y = 16$.

so $(8, 0)$ means this point will be $(8, 0)$ and $(0, 12)$ and this point will be $(0, 12)$.

join these two point

so this line will represent $3x + 2y = 24$ then point $(5, 0)$ this point is $(8, 0)$ and this point is $(0, 12)$ now $(5, 0)$ so this point will be $(5, 0)$ and $(0, 15)$ this point will be $(0, 15)$ so join this two points

so equation of line $3x + y = 15$ now $x = 4$

so $x = 4$ is a line passing through $(4, 0)$ and parallel to y axis see $x = 4$ now let us consider or given inequalities $3x + 2y \geq 24$ now for one that is $3x + 2y > 24$

so origin test means we have to check whether origin lies in the region or not so put $x = 0$ and $y = 0$.

so $3 \times 0 + 2 \times 0 = 0$ is greater than equal to 24 which is not true

so origin does not belong to solution reason it means for this $3x + 2y \geq 24$ the reason will be this because in this region origin does not lie

so this will be the reason this will be the reason now for second that is $3x + y \leq 15$

so put $x = 0$ and $y = 0$

so $3 \times 0 + 0 = 0 \leq 15$ this is true

so origin belongs to solution reason it means for this $3x + y = 15$ the solution will be reason will be this solution region will lie in this direction now for $x \geq 4$ that is x greater than equal to 4 it means $x \geq 4$ means all the value of x which is greater than equal to 4 now for different inequalities we have different solution reason now we have to find which reason will be the common reason or whether common reason will exist or not

so in this case we have

so according to defined reason for different given inequalities no reason will be common reason

so solution reason will be phi means if you said for this and set with different color

so we see that no reason which contains all the three colors means blue green and red

so for this system of given inequalities we have no feasible region or no solution region

so solution region will be empty set now let us consider another example solve graphically $2x + 3y \leq 12$, $x \geq 2$, $y \geq 1$ solution say this is first this is second and this is third

so associated equation $2x + 3y = 12$, $x = 2$, $y = 1$ associated equation 1, 2 and 3.

now $2x + 3y = 12$

so put $y = 0$ implies $x = 6$, $x = 0$ implies $y = 4$

so points are $(6, 0)$ and $(0, 4)$ it means this line intersect x axis at 6 and y axis at 4. second $x = 2$ is a line parallel to y axis and passing through 2. for $y = 1$ is a line parallel to x axis and passing through 1. now draw the graph of all these three lines x axis y axis 0 1 2 3 4 5 6.

one two three four

so for first line we have point $(6, 0)$ and $(0, 4)$ so join these two point

so this will be line $2x + 3y = 12$.

now $x = 2$ is a line parallel to y axis and passing through 2.

$x = 2$ and $y = 1$ is a line it says $y = 1$ now we have to define its solution region for different inequalities

so for this we just check origin test origin test

so $(0, 0)$ that is $2x + 3y \leq 12$ put $x = 0$ and $y = 0$

so $2 \times 0 + 3 \times 0 = 0 \leq 12$ is true

so $(0, 0)$ lies in the solution region reason for $2x + 3y \leq 12$ for second $x \geq 2$

so solution region lies in right hand side of line $x = 2$ and four

three that is $y \geq 1$ implies solution region lies in upper part of line of the line $y = 1$ now define region accordingly in the graph

so for $2x + c y \geq 12$ origin lies it means this will be the solution region for in equation $2x + c y \leq 12$ now for $x \geq 2$ the right hand side of the line $x = 2$

so this will be the solution region for $x = 2$ now for $y \geq 1$ this will be the solution region now combining these three region will get this region and this solution region and this solution region

so this triangle abc will satisfy all the three inequality so this shadow region will be the solution region for the given system of given system of in equation $2x + 3y \leq 12$ $x \geq 2$ and $y \geq 1$

so we can finally write shadow region abc will satisfy all the three given constants

so solution region will be the shadow region abc

so in this way we can find the solution region for the given different inequalities now consider another example that is solve graphically $x + 2y \leq 8$ $2x + y \leq 8$ $x \geq 0$ $y \geq 0$ solution associated equation for say this is one this is two and this is three for first second first and second

so $x + 2y = 8$ and $2x + y = 8$ put $y = 0$ implies $x = 8$ $x = 0$ implies $y = 4$

so points are $(8, 0)$ and $(0, 4)$ for second $2x + y = 8$ put $y = 0$ implies $x = 4$ and $x = 0$ implies $y = 8$

so points are $(4, 0)$ and $(0, 8)$ $x \geq 0$ and $y \geq 0$ implies first quadrant means in first quadrant both x and y are positive

so $x \geq 0$ and $y \geq 0$ is a condition for first quadrant now draw the graph of these two associated equations $x = 2, 4, 6, 8, 10$ $y = 2, 4, 6, 8$

so points are $(8, 0)$

so this point is $(8, 0)$ and $(0, 4)$ and this point is $(0, 4)$

so join these two points this will represent $x + 2y = 8$ this is $(8, 0)$ and this is $(0, 4)$.

now $(4, 0)$ and $(0, 8)$

so this is $(4, 0)$ and this is $(0, 8)$ again join these two points and this will represent line $2x + y = 8$ and this point is $(0, 8)$ and this point is $(4, 0)$ to define the region we have to again check origin test

so origin test for $x + 2y \leq 8$ put $x = 0$ $y = 0$ imply $0 + 2 \times 0 \leq 8$ is true

so origin

so $(0, 0)$ belongs to solution region for $x + 2y \leq 8$ put $x = 0$ $y = 0$ implies $2 \times 0 + 0 \leq 8$ is again true origin belongs to solution region

so origin lies in solution region of both the in equation $x + 2y \leq 8$ and $2x + y \leq 8$ now define the solution region in the figure this is $x \geq 0$ and this is $y \geq 0$ origin lies in the region

so origin lies in the region origin also lies for solution region of this

in equation now combining this condition it means here

so solution region is here this is a it means this part will be the solution reason for the given indication or you can say common reason for the given system of inequation and name it as this is a this is b and this is c

so solution reason common solution region for the given given system of inequalities one two and three will be shaded region o a b c let us take another example solve graphically $x + y < 5$ $4x + y > 4$ $x + 5y \geq 5$ $x < 4$ $y \leq 3$

so here we have five linear inequities and we have to solve these five inequalities simultaneously

so say this is one this is 2 this is 3 and this is 4 and this is 5.

associated equation equation for given in equation 1 2 3 4 and 5 are $x + y = 5$ $4x + y = 4$ $x + 5y = 5$ $x = 4$ $y = 3$ the four one $x + y = 5$ put $y = 0$ implies $x = 5$ $x = 0$ implies $y = 5$

so points are five zero and zero five four two four $x + y = 4$ put $y = 0$ implies $x = 1$ $x = 0$ implies $y = 4$ $4x + 5y = 5$

so put $y = 0$ implies $x = 5$ and $x = 0$ implies $y = 1$

so points are one zero and zero four points are five zero and zero one four fourth $x = 4$ is a line parallel to y axis and passing through four zero $y = 3$ is a line parallel to x axis and passing through zero three now after discussing all the five associated equation we are able to draw the graph of this equations x axis y x is 0 1 2 3 4 five six one two three four five six minus one minus two minus one minus two

so four $x + y = 5$ points are five zero and zero five five zero and zero five

so join these two point $x + y = 5$ five zero and this is zero five for four $x + y = 4$ points are one zero and zero four one zero and zero four

so join these two points this is one zero and this is zero four for third equation $x + 5y = 5$ points are five zero and zero one five zero and zero one

so join these two points $x + 5y = 5$ and this line is four $x + y = 4$

so this is point zero one is five zero now $x = 4$ is a line

so $x = 4$ is a line parallel to y axis and passing through 4 0.

so this is $x = 4$ and $y = 3$ is a line parallel to x axis and passing through zero three

so this is $y = 3$ now let us check the inequality

so first inequity is $x + y \leq 5$ it means this line sim says $x + y \leq 5$

so this line is half line

so this line is not full line this line is half line and $x + y < 5$

so when you check origin test you will find this region will be the solution region this region will be the solution reason again for second inequality if you again go through origin test you will find this reason will be the solution reason and for third inequities if you go through the origin test you will find this region will be the solution region and four fourth $x < 4$ for $x < 4$ this will be the solution region and for y

less than equal to three downward reason will be the solution reason when you combining all this reason

so this is solution region this is solution region and this is solution reason and this is solution reason and this will be the solution region

so four five in utility we have these five common solution region which satisfy by this shaded region

so say this is a this is b this is c this is d and this is e

so this region having this boundary line is not included this boundary line is not included from this to this point this is open

so this is open reason not closed reason

so finally we can say common common reason for all the given in utilities 1 2 3 4 and 5 will be the shaded region a b c d e hence solution region will be region a b c d e

so in this way we can solve many in equation simultaneously and find common reason or solution reason for the given inequalities simultaneously okay thank you you