

so let's start with today's class just where we left off uh yesterday remember we were talking about so this was lecture number seven and yesterday the last part of lecture number six we were talking about the units of rate constant right and you know for a first order reaction we found that the unit of rate constant would be the inverse of time that is either inverse of second minutes hours right if you go for a second order reaction so it would be like this litter mole inverse time inverse making sure that whichever is having the positive exponent is written at the very first and then ah you go to a zero order reaction so for the zero order reaction what happens is the rate is equal to  $k$  times ah the concentration of the reactant raised to the bus zero that means rate is equal to  $k$  so whatever the unit of rate is that turns out to be the unit of  $k$  the rate constant we did a very quick example and the example was that if you are given a reaction where both  $a$  and  $b$  are involved as the reactants and it is told to you that the reaction is first order with respect to  $a$  and first order with respect to  $b$  then can you write the rate expression you assume the time to be in minutes ok so this was the last thing we did yesterday where we saw that if we have this as given according to the question rate is equal to  $k$  times  $a$  raised to the power one concentration of  $a$  raised to the power one concentration of  $b$  raised to the power one then the overall order is one plus one equal to two and then what is the unit of rate constant the unit derivative constant then turns out to be the unit of rate over the unit of the concentration of  $a$  times unit of the concentration of  $b$  and hence this is what we end up with now quickly if you do ah you know if we ah do you know one more thing which is suppose we take another example rights continuation of the same thing we say this is example b ok we have a reaction ok between  $a$  and  $b$  ok so these are the two reactants and it is again said that the reaction is first order with respect to  $a$  and ok say second order with respect to  $b$  ok so then when you write the rate expression so the rate expression obviously becomes like this is equal to  $k$  which is rate constant times concentration of  $a$  raised to the power one because it is first order consideration of  $b$  raised to the power two because it is second order hence  $k a b$  plus bar two and then based on this i can write that the overall order of the reaction is one plus two equal to

three

so now having you know discussed about these it should be straight forward to you why it is one

plus two equal to three this being the overall or total order of the reaction ok now what

about the units of rate constant

so the units are rate constant would be then  $k$  equal to rate over concentration of  $b$  squared right

so i can write you know what rate is

so rate is concentration over time here the time again you assume the time to be in minutes

so it would be mole liter inverse mini inverse and then i will be having i can say mole liter there is a unit of consideration

of  $a$  and in this case i will be having mole liter raised to the bar two why because

it is second order right

so here now as you will ah realize that the first mole liter and this one cancels out and i will be left with liter squared mole to minute minus one

so then this would be the unit of the rate constant  $k$  okay and again what you should pay attention to is that i have

written letter raised to the power 2 as the first term why because here i have the positive

exponent and then the negative ones come later you know hopefully now you can ah given a

certain rate expression or given a question like this you would be able to find out the

rate expression write the rate expression find the total order of the reaction and then even

go ahead and find the units of the rate constant having looked at rate expression and

also having looked at the rate constant you must be wondering about this what is the significance of rate and rate constant well what i mean by this will ah soon

be clear you know when i go ahead with this topic now what happens is because rate

depends upon the concentrations

so rate will vary with the concentrations of your reactants ok

so the rate will vary with the concentration

of reactants then what it becomes is a problem when if you are trying to compare you know reactions why because if you change the concentration the rate will change right

so what i can say is this the rate is not of much use

again the rate is not of much use in quantifying in quantifying reactions or comparing reactions right

so this is important

because it says the rate is not of much use well it it makes sense right because the moment

you change the concentration the rate will change comparing reactions you know the concentrations if

they differ then again you cannot compare the rate however there is way out what is the way

out well the way out is you realize now what i am trying to tell you or what i am

trying to ah reach at is that the rate constant is a constant at a given temperature right and is independent independent of the concentrations concentrations of the reactants ok there are few important terms out here

so the rate constant is a constant at a given temperature this is important because

rate constant does depend upon temperature you know the Arrhenius equation which will

come to later and also it is independent of the concentrations of the reactants

right hence you can see as opposed to rate can easily be used that means the rate constant

can easily be used to sorry to quantify and compare reactions ok

so while rate of the reaction is in some sense useless because it depends on the concentrations but the rate constant at any given temperature is independent of the

concentration of the reactants and hence you can always use to quantify or compare certain

reactions or compare reactions not only that if you know the rate constant and the order of the reaction you can easily write down the rate expression right

you can easily write down the

rate expression for that reaction ok

so because you know what is rate is equal to

say  $k$  times concentration of a raised to the power  $n$  like we had done before say rate is equal

to  $k$  times concentration of a the reactant raised to the power  $n$  which is the order

so if

you know the rate constant  $k$  if you know  $n$  then you easily write down the rate expression

so that

was in some sense the significance of the rate and the rate constant ok you can understand the

rate constant is fundamentally much more useful because of the fact that it is a constant

independent of the concentrations but do keep in mind it does depend upon temperature so

if you are comparing two different reactions you better compare them at the same temperature

because rate constant would otherwise differ whatever we have done up till now in you

know when we are talking about the rates you know the average rate the instantaneous rate and

all these things we were mostly focusing on what drawing of tangents right but the drawing of

tangents ah is you know not always advised right

so for this what we do is

we go for something known as integrated rate law integrated weight loss or integrate rate or i can write rate equations ok integrated

rate equations or rate expressions whatever

so i was telling you this up

till now what we did was to find say suppose i would like the instantaneous

rate ok

so suppose i am given a kinetic profile like this ok

so this is the concentration of a versus

time t and someone would tell me ok fine ask me find the instantaneous rate somewhere here

what i would do is i would actually then draw a tangent and then try to find out the instantaneous

rate but then the problem is that how accurately you draw the tangent will determine how

accurately you figure out the instantaneous rate that is why this is not the preferred way of doing

it all the time however however keep this in mind that if you are going to have you know complex reactions which means the reaction is not

straight forward or there are secondary reactions you know you know it makes ah the whole

reaction scheme very complicated then obviously the way you would figure out say the instantaneous

rate by drawing a tangent or the initial rate by drawing a tangent at the initial point

would still be the more favorable ah way of calculating the rate of the reaction

but however for reactions which are relatively straight forward we would

rather not use the tangent expression or you know the ah the method of drawing the tangent

and then figuring out the rate instead we would do something which is related to this title

the integrated weight loss or the integrated rate equations ok now this is ah you know one of

the main aspects of chemical kinetics from where based on the integer weight loss you can

do a lot of manipulations lot of things but before i go to indicate weight loss i would

like to bring to your notice a very important aspect or a very important parameter in

chemical kinetics its called half life for a given reaction now why was this concept necessary and why or in what sense

is it useful now again suppose you are given a kinetic profile like this where this is the

concentration of the reactant and this is the time okay now yes one thing is that i can go and derive

the indicated rate expression and work based on that but if i want to take a step back and based

on this kinetic profile i want to say something at the preliminary level about this reaction can

i do that and if i can what would i base it on what is that value what is that term what is

the parameter that i would base my initial value or my initial you know focus initial

explanation which would lead me to some deeper insights about this corresponding reaction without

having to go to the integrated rate expressions

so that is why this half life

was some sort of a preliminary check based on the kinetic profile

so that means based on

this kinetic profile as you see can we say something about the type of the reaction

that you have or your study ok

so then this importance of half life was first coined by wilhelm ostwald he was awarded the nobel prize in nineteen o nine he was at the nobel prize in nineteen o nine and he was earn an old prize mostly for his work on catalysis and also for ah providing many of the fundamentals of chemical

equilibrium and chemical reactions kinetics

so willem oswalt

so this would be l

sorry wilhelm osfald was the first person who said that half life at the preliminary level

would already tell us or provide us appreciable or significant information about the reaction

that we have in our hands or that we are studying

so let us go and try to see what this concept of half life is

so when we say you know when we say half life what we mean by that is that or we

are trying to define half life right

so half life this is the time

so remember its half life half life is defined in terms of the time

so this is the time it takes it takes for the concentration the concentration of the reactant

so again what is half life half life is the time it takes for the concentration of the reactant to fall to one half one half of its initial value

so again what is half life half life is the time it takes for the concentration of

the reactant to fall to one half of its initial value now this is important ok how

do we visualize this on the graph itself or the kinetic profile itself again as usual let us draw a kinetic profile ok

so as we always say this is the concentration of the reactant

the reaction being a and this is time whatever unit it be seconds

minutes hours now suppose we have a profile which goes something like this ok

so this is my reaction profile or kinetic profile for a certain reaction ok now this value

so this would be time 0 for me exactly the initial time

so this value

out here is my

so i can write here this is a zero

so what is a zero

so then a zero is the initial value of the reactant

so that means at the

moment the reaction is starting the value of this reactant is a zero

as zero refers to time zero then by the definition of half life if you remember by the definition of half life the half life would be the time it takes for the

concentration of the reactant to fall to one half of its initial value

so if this is zero this

is a naught somewhere here then this comes to half a naught right its not

exactly drawn to  
 scale but when it comes to half a naught is half a naught this time from here to  
 here is  
 called  $t_{1/2}$  well i will come back to this again now what you can also figure  
 from here is that  
 if i have having half a naught  
 so from here to here i can again come to half of it  
 so let  
 this be  
 so let this be  $t_{1/2}$   
 so let me put this ok  
 so then this is one fourth a naught right and i can even go and say that ok  
 this is half of this gap  
 and i can write one eighth a naught ok  
 so just let me  
 complete this then i will explain what i am trying to achieve out here right ok  
 now lets look at this  
 so let this  
 so let this be corresponding intervals time intervals and remember i have my  
 time access on  
 the x axis the time on my x axis right so  
 so now look from a naught the half life  
 says that is the time required to go down to half of the concentration of a  
 naught  
 which is half a naught  
 so this would be my  $t_{1/2}$  i can say one i will tell you why i am  
 saying one now again when i reach half a naught  
 so then between zero and half a naught i can  
 again again decrease the concentration by half which will become one for a  
 naught  
 so this  
 one for a naught would be my next time right  
 so from here to here  
 so for example from here  
 to here you can see i can write this is  $t_{1/2}$  two right and again this would be  
 $t_{1/2}$  three  
 ok  
 so which i did not mention before  
 so this  $t_{1/2}$  is referred to as the half life thats  
 the symbol of half life that we always use right when i go from a naught to  
 half a  
 naught the time it takes me to go half to go to half of my initial  
 concentration is  
 $t_{1/2}$  right now we see here in red i have written  $t_{1/2}$  one  $t_{1/2}$  of one means  
 again if  
 i write here  $t_{1/2}$  of one means the first half life then whatever  $t_{1/2}$  two  
 $t_{1/2}$  of  $t_{1/2}$  is the second half life what is the second half life second of life is  
 the time it takes my concentration to fall from half a naught to half of half  
 a naught which  
 is one fourth a naught  
 so then  $t_{1/2}$  two is my second half life and likewise  $t_{1/2}$  three is my  
 third  
 half life right the concept of half life is the same what is it it tells you  
 at the time it takes

for me to go to half of the initial concentration of the reactant right  
 so if my initial concentration is  $a$  then the time it takes for me to go to half of  $a$   
 is  $t_{1/2}$  one which is the first half life why is first half because  $a$  is the  
 initial concentration i am starting with now when i go from half  $a$  to half of that  
 so if now half  $a$  is my initial concentration right and then i am going to half of that which is  
 one fourth  $a$  then the time taken for that is  $t_{1/2}$  two  
 so it is my second half life then again half of one fourth  $a$  which is one eighth  $a$   
 then the time taken to go from one fourth  $a$  to half of one fourth  $a$  which is one eighth  $a$  is my  
 third half life  $t_{1/2}$  of three ok  
 so as you can see from this kinetic profile you will be able to figure out  
 based on the manner in which the concentration of the reactant is decreasing  
 where the first second and third half lives would be generally when we say half life you  
 always be in the first half life that's what talking about unless and until it is specifically  
 mentioned to you you know go for the subsequent the second half life or the third half life and  
 so on the first half life is the one we generally consider and that's what we will mostly focus on and  
 when i say half life that's typically what i mean the first half life right  
 so yes from this you know kinetic profile what we now know to do is given the starting reactant concentration  
 given the manner in which it decreases the concentration reaction decreases as a  
 function of time we will be able to figure out from this experimental curve what my half life would be  
 now what is the significance of this you know why we consider this to be a preliminary  
 check it would not be clear right now to you ah it will only become ah more clear or  
 clearer if i ah start discussing about the integrated rate expressions or the integer  
 rate laws and then bring this consider half life ah in and make the connection but at least  
 let me tell you this if you consider you know this kinetic scheme though it is not drawn to  
 scale but what you would realize qualitatively that this  $t_{1/2}$  one is equal to  $t_{1/2}$  two is  
 equal to  $t_{1/2}$  of three which means that no matter no matter at what point of this reaction you are  
 the half life is always the same that means the half life is independent of the concentration of your  
 reactant right so let me you know write this again what i am saying out here is remember we  
 said that the

half life can be a preliminary check what did i mean by that what sort of insights can i get by looking at the way the half life is changing as a function of the progress of the reaction

right

so what i mean is what i mean is this that if it has to be a primary check i need to get

something out of it if you look at this the  $t_{1/2}$  one is equal to  $t_{1/2}$  two is equal to  $t_{1/2}$  three right if this happens that

means the half lines are all equal if that is the case then what we say is this is a unique signature of a first order reaction ok its a unique signature of first order reaction so that means if the half lives are independent of

the reactant concentration it remains the same throughout right does not matter at what point

of the reaction we are in hence if we can figure this out we can immediately say without doing

anything else that this is a first order reaction ok with respect to the reactant hopefully i have

realized that this half life can be very important as we said that the successive half lives right so

these are your you know you can say these are your successive half-lives which are equal to each other being the signature of the first order

equation and as i said it is independent of the concentration of the reactant so when

we go and discuss about the integrated rate equation for the first order ah reaction we

should be able to see this again right ok now lets move on to the thing we started with the

integrate rate expression

so lets start with one of the simpler ones which

is a zero order reaction ok let us start with this now this obviously very simple

so what we say is that as per definition of the zero order reaction the rate the rate of

the reaction is equal to  $k$  if  $a$  is the reactant  $k$  times consideration of the reactant raised

to the bus zero  $a$  being the reactant ok

so this anything raises one zero is equal to one therefore

rate is equal to  $k$  let this be equation one um ok now also also from the definition of a

rate it is very important to understand that the way the rate is defined is  $-\frac{d a}{d t}$

ok this is my definition of the rate what i am saying i am considering a reaction where  $a$  is going to be ok now this  $-\frac{d a}{d t}$  then

is equal to  $k$  let this v 2 right now what we will do is we will say that ok then i can

write this again as  $-\frac{d a}{d t}$  is equal to  $-k a$

so i have two sides two variables one

is depend upon the consideration of  $a$  the other one is depend upon the variable  $t$  which is time okay

so what we will now do is we will integrate both sides we will integrate both sides

so which means  $-\ln a$  is equal to  $-k a t$  and what do

we integrate in between we indicate between  $t$  is equal to zero  $t$  is equal to zero that means  
 the initial time reaction is not yet started or just about to start with  $t$  is equal to  $t$  so  
 this is my interval  
 so for the time my initial time point is zero and the final time point is any arbitrary time point  $t$  ok then what about the limits of the integration for  $a$  there is a  
 constant of the reactant  
 so time zero i say the concentration of my reactant which is my initial concentration is given as  $a$  naught not corresponding to  $t$  is equal to zero then as i go  
 at time  $t$  i can say that my concentration of  $a$  can be represented as  $t$   
 so if that  
 is the case then i go ahead and do the integration keeping in mind that  $k$  is a constant let this be equation four  $k$  is a constant and can be kept outside the integral right and can be kept outside the integral if that is so then  
 immediately this what this becomes is see i integrate this the first one on the left hand side it would be  $a$   $t$  minus  $a$  at time is equal to zero is equal to  
 minus  $k$  then it would be  $t$  minus zero right ok or i can write it again as  $a$   $t$  minus  $a$  naught  
 my initial reactant is equal to minus  $k$  of  $t$  or  $a$   $t$  is equal to  $a$  naught minus  $k$   $t$  let this be five ok  
 so what does this tell me this tells me that once i have integrated once i have indicated my what did i start from my zero order reaction  
 with  $a$  going to be once i have integrated that and i have set up my equations like this then  
 i did the integration within the defined limits right a definite integral within the defined time  
 limits for  $t$  is equal to zero my concentration is  $a$  naught the initial concentration for  $t$  is  
 equal to  $t$  my concentration is consideration of  $a$  at time  $t$  as defined by this integral right  
 and hence when i go ahead and do the integral i end up with an equation like this the  
 moment you end up with an equation like this you still realize oh this is a straight line equation right doesn't it look like  $y$  is equal to  $m$   $x$  plus  $c$  right where  $y$  is  $a$   $t$   $c$  intercept is  $a$  naught  $x$  obviously is  $t$  and  $m$  is equal to minus  $k$  so  
 $y$  is  $t$   $c$  is  $a$  naught  $x$  is  $t$  and  $m$  actually is minus  $k$  right  
 so this is the equation of straight line if i want to plot a graph how would the plot look like  
 so the plot would look as you have rightly guessed if this is  $a$  this is time ok here consideration of  $a$  at time  $t$  is  
 equal to consider  $a$  naught minus  $k$   $t$   
 so this would be a straight line straight line with the significance that this is my intercept which is my  
 initial consideration  $a$  naught because this one corresponds to time  $t$  zero and then the slope the slope is equal to minus  $k$

based on based on the equation  $a_t$  is equal to  $a_{naught} - kt$   
so this  
is the equation i have plotted out here right the equation of a straight line  
with a  
negative slope because the slope is negative the because the slope is negative  
the negative  
slope is equal to minus  $k$  and from there i get  $k$   
so i get the rate constant  $k$  and  
one more important thing is that if for a reaction if for a reaction this  
profile is maintained that means if plot of the concentration of  $a$  versus time  $t$   
is a straight line straight line as we see with the negative slope then then  
this is the signature then this is the signature of a zero order  
reaction ok  
so then this is the signature of a zero order reaction now this is  
extremely important to keep in mind ok so you might be you might not be given  
anything you  
just might be given a graph plotted like this and you might be asked what type  
of a reaction does it  
signify and that is what you have to say or that is what you have to keep in  
mind while you give  
the answer  
so which means again that if it is zero order kinetics or the reaction you  
are studying  
follows zero order kinetics then the plot of  $a$  versus  $t$  there is a consideration  
of  $a$  at time  $t$   
versus the time  $t$  should be linear like this and as i said again the slope  
being negative by itself  
this is equal to minus  $k$  right and hence you get  $k$  which is a positive value  
the rate constant  
right and that is why this graph is giving you ok  
so that was about you know the indicated rate  
expression and the plot plots are very useful for chemical kinetics because as  
i was saying  
even for a half life plot even in a half life from a kinetic reaction profile  
or the plot  
from a zero order reaction you would be able to figure out what type of  
reaction you are talking  
about ok now lets consider the half life right  
so lets consider the half life for a zero order reaction let us consider the  
half life now  
so we discussed half life before ok let me see what ah my initial the ending  
equation was ok  
so the ending equation was five  
so the next equation number would  
be six i often you know ah miss or lose track of my equation numbers but  
anyway let  
us consider the definition of half-life now right  
so the definition was like this if my  
initial concentration is  $a_{naught}$  then the half-life which is my first  
half-life and i said  
the half life we are going to refer to is always the first half life is the  
time it takes to go to  
half of  $a_{naught}$  right that was the interpretation or that was the definition  
of half-life

so let us go back to this equation five where we had a of  $t$  is equal to  $a - kt$

so this was equation five form right

so now what happens at  $t_{1/2}$  what happens at  $t$  out that means if this  $t$  is now  $t_{1/2}$  because i am trying to figure out the expression for half life from this rate equation

right if i trying to do that what i say is that  $a - kt$  at  $t$  is equal to  $t_{1/2}$  at  $t$  is equal to

$t_{1/2}$

so this remains the same  $a$  is always my initial concentration at  $t$  is equal to  $t_{1/2}$

so my half life what changes is in this equation is one is  $t$  is replaced by  $t_{1/2}$  and the other thing is  $a$  gets replaced by half that is  $a$  gets replaced

by half  $a$  because thats what the definition of  $t_{1/2}$  of  $s$

so  $t_{1/2}$  is what  $t_{1/2}$  is the time it

takes for the consideration of the reactant to go to or to fall to half of its initial value

or half of its starting value

so you keep this as six you know once we have this we can easily rearrange and write that  $kt_{1/2}$  is equal to  $a - \frac{1}{2}a$  right and

so based on this i can go forward and write that  $t_{1/2}$  or  $kt_{1/2}$  is equal to half  $a$  right

so  $a - \frac{1}{2}a$

$a - \frac{1}{2}a$  is half  $a$  and hence  $t_{1/2}$  is equal to  $a$  by two  $k$

so this is a very important relation for the half life

of a zero order reaction speed seven what does this tell you what it tells you is the half life is directly dependent upon the concentration of the reactant

so greater the

consideration of the reactant greater than of life now why do i say it is only depend on the

concentration react well it does depend upon  $k$  but do realize that for a given

reaction  $k$  at a certain temperature is constant and two is obviously a constant right so

essentially what i am going to say is essentially it is depending upon the concentration

of  $a$

so this is what we can write the half life the half life for a zero order reaction is proportional to the concentration of the reactant right is proportional to the concentration of the reactant so

that means higher the concentration higher the half life lesser the concentration lesser the

half life right that means again based on this higher concentration means higher

half life ok in other

words as a reaction proceeds and if that reaction is of zero order

here we are talking about zero order reaction right now because everything is under the that description of a zero order reaction

so as a reaction proceeds and

if it is following zero order then the half life also decreases then the half

life also decreases  
right which makes sense again because what happens is the reaction proceeds  
what happens is  
the reaction proceeds is that my concentration of the reactant is decreasing  
right now you can take  
a naught you know you can take this a naught like a naught going to half a  
naught right and half  
a naught what has happened is it is already less than a naught right now if  
you go from half  
a naught to one fourth a naught see what is happening is you are decreasing it  
even more half  
a naught is less than a naught one fourth a naught is even lesser than half of  
a naught right  
so what  
it means is if you are going to calculate  $t_{1/2}$  right then  $t_{1/2}$  the first  
half life would be  
having the maximum value when you go to  $t_{1/2}$  two which is the second half  
life which is the  
time it takes for you to go from one half or half of a naught to one fourth a  
naught because  
the concentration has decreased from a naught to half of a naught the half  
life will also decrease  
ok and  
so on and hence as the reaction proceeds the concentration the reaction  
decreases  
and  
so does the half life this is very characteristic feature of a zero  
order reaction now recall our concept of recall or concept of half life being  
used as a preliminary preliminary check ok and this is what was meant  
so what was  
meant was that for the zero order reaction for the zero order reaction if it is  
zero order reaction if it is zero order  
reaction then as the reaction proceeds the half life decreases if you have  
so now conversely  
if you are given a reaction profile right if you are given a kinetic profile  
and from there  
you are seeing that the half life is decreasing as a function of time that  
means  
as the reaction is progressing then you immediately say that as a preliminary  
check because the half life is decreasing as the reaction is proceeding it  
means that it  
should correspond to a zero order reaction or that the reaction i am looking  
at follows  
zero order kinetics right hopefully now you know having discussed half like  
before we  
started this integrated rate laws or integrate equations that i was telling  
that half life can  
be used as a preliminary check then we moved on to the zero order integrated  
out got this  
linear dependence of the concentration on time negative slope from the slope  
is this you get  
minus  $k$  and hence you get  $k$  being a positive quantity but then you see half  
life it decreases  
as a reaction is progressing and then it tells you as again a preliminary

check i am using this word  
each and every time having not done anything else just using the half life you  
are able to take  
tell that this reaction must follow zero order kinetics ok  
so you can see that ah you know today  
in this class we have entered this ah realm of integrated rate laws or  
indicate rate equations  
we are done with the zero order rate equation so what we will do is in the  
next class we will focus  
on the first order and second order rate equations and then again move on from  
there and discuss the  
other aspects of chemical kinetics ok thank you you

Prutor@uittk