

welcome everybody to this class this is a lecture five on chemical kinetics we will start from where we had left off in the previous class and if you would remember that in the previous class we had introduced a concept referred to as the degree of advancement of a reaction and we were monitoring $d\xi$ so that was ξ is the degree of advancement of the reaction over time that is dt so at the end of the class nearing the end of the class this is where we had left off what we had started to do this was the reaction we were looking at acetaldehyde going to methane and carbon monoxide then we said we assume ideal gas behavior assuming ideal gas behavior we write the initial number of moles we say that this is the progress of the reaction the progress of the reaction being denoted by the extent of the reaction which is ξ or the degree of advancement of the reaction once we are done with that we started writing down the number of moles of each and every species so this was the number of moles of acetaldehyde and zero C_2H_4 or $n_{C_2H_4}$ has to say $n_{C_2H_4} - \xi$ why it is minus because we are losing the reaction or reactant then $n_{C_2H_4}$ is equal to ξ y again this one is equal to ξ number one n_{CO} there was no product to start with CHO was not there and then because it is a product you are gaining it as a function of time it is having a positive value and the coefficient is one so it is $n_{C_2H_4}$ is equal to ξ and same we are having n_{CO} which is also equal to ξ then what we have is initial number of moles the initial number of moles is $n_{C_2H_4}$ C_2H_4 is equal to $n_{C_2H_4}$ so that is what it is right where zero or not represents the initial number of moles and $n_{C_2H_4}$ to the C_2H_4 essentially is what $n_{C_2H_4}$ C_2H_4 means that this is the only species that i have i have present at the start of the reaction now then how can i write the total pressure so the total pressure can be written as follows so the total pressure is equal to so this is equal to the pressure from C_2H_4 the pressure being exerted by methane and the pressure being exerted by carbon oxide now again remember that we are taking the ideal gas assumption where ideal gas means $p \times v$ is equal to $n r t$ where n is the number of moles so having done this having done this what i can do is i can write $p_{C_2H_4}$ is equal to the number of moles of acetaldehyde which is $n_{C_2H_4} - \xi$ right into $r t$ by v so this is what we are

doing

so ideal gas pV is equal to nRT what is n for acetaldehyde is n_0 right

so this is $n_0 - \xi$ because ξ is the extent by which the reaction is progressed times R/T by V

so this is what we have p_{CH_2O} is

equal to $n_0 - \xi$ times R/T over V likewise we can write the same for p_{CH_4} this

is equal to $\xi R/T$ over V why because ξ is the number of moles of methane and then the same for

carbon monoxide is $\xi R/T$ over V ok now having written this now we can go for expression of the

total pressure

so how do i write that then i can write remember the total pressure p_{total} is

equal to $p_{CH_3CO} + p_{CH_4} + p_{CO}$ right sum of all the components present in

the reaction then we already have expressions for each of these p_{CH_2O} , p_{CH_4} and p_{CO}

we just wrote those down

so i can write that as $n_0 - \xi$ this is the number of moles of CH_2O plus ξ the number of moles of methane plus ξ the number of moles of carbon monoxide

times R/T over V

so what did we do out here we essentially just added all these up $p_{CH_2O} + p_{CH_4} + p_{CO}$

plus p_{CH_4} plus p_{CO} right by V is a constant R/T because temperature is a constant volume

is a constant and hence i can take R/T by V out as a common factor

so that's what i have done

then p is equal to $n_0 - \xi$ plus ξ plus ξ times R/T over V

so then i can write p is

equal to n_0 sorry n_0 plus ξ then R/T over V i can further simplify this by writing n_0

R/T over V plus $\xi R/T$ over V now this is a significant point or this is a significant step

in the reaction

so if you would realize this component has n_0 times R/T over V n_0 is was the initial number of moles

so remember see if i write it here n_0 was the initial number of moles ok

so n_0 was the initial number of moles

if that is

so then i can say that this one is the initial pressure which we can say is p_0

so the

initial pressure is p_0

so p_0 is equal to $n_0 R/T$ over V plus this $\xi R/T$ over V

so p now can be further written as the p can be further written as that is the

total pressure can be further written as p is equal to p_0 which is the initial

pressure plus $\xi R/T$ over V now what we do is we look at it take the differential form of it

you know you know differentiated with respect to t
 so the total pressure which is equal
 to $\frac{dp}{dt} + \frac{p}{v} \frac{dv}{dt}$ if we do that now p
 is a constant right
 so I can say p is a constant because the initial number
 of moles is n which is a constant hence this one is equal to zero thus
 the equation gets
 simplified to $\frac{dp}{dt}$ there is a rate of change of pressure with time
 is equal to $\frac{r}{v}$
 $\frac{r}{v}$ is a constant t has been kept constant v is also constant
 these were the initial
 conditions of the reaction $\frac{dp}{dt}$ right hence I can further write
 this one as
 so let me write this again on the next page
 so what we just had was $\frac{dp}{dt}$ is equal
 to $\frac{r}{v}$ by $\frac{dp}{dt}$ or $\frac{dz}{dt}$ right hence I can say that one by
 $v \frac{dp}{dt}$
 is equal to one by $r \frac{dp}{dt}$
 so this is what we were aiming for and the problem so
 what have we done we have looked at the change in the extent of the reaction
 so we have looked
 at the change in the extent of the reaction which is $\frac{dz}{dt}$ this
 times one by v is a
 constant is equal to one by $r \frac{dp}{dt}$ that means that means if I
 follow the change of
 pressure with respect to time that is equivalent that is equivalent to
 following the change
 of the extent of the reaction as a function of time and this one by v times $\frac{dz}{dt}$
 $\frac{dz}{dt}$ is what nothing but the rate of the reaction and thus we say that the rate
 of the reaction can
 be monitored by monitoring the change of pressure with respect to time the
 only thing is there is
 there are these constants one by r because these were kept as constants
 so thus this example shows
 you how to incorporate or how to you know express the rate of a reaction in
 terms of the change of
 pressure in a gaseous reaction the example being the one we were discussing
 right now
 so hopefully
 by doing this exercise or rather an example you would understand the essence of
 this $\frac{dp}{dt}$
 the degree of advancement of the reaction and the utility of the same in
 expressing the
 rate of the reaction in terms of whatever you want it to be whether it is a
 concentration
 or in case of gaseous reactions whether it is the pressure
 so now what we will do is having
 established this concept of rate in terms of $\frac{dp}{dt}$ having looked at operational
 definitions of
 rates of reactions in terms of the coefficients and changes what we will now
 do
 is we will now look at something which is much more widely used that
 means we are slowly taking a step into the crux of chemical kinetics which is

our kinetic analysis and rate equations

so then i start this section by writing kinetic analysis of experimental data
ok and we will soon realize what it means

but in short the significance is that when i am doing an experiment on or
related to chemical kinetics i

am following the rate of change of concentration either of reactants or
products

as a function of time i generate some plots and what we will see is what do
those

plots help us in interpreting in terms of the different definitions of rates
which are

out there

so let us look at this one first what we will you know try to discuss out

here is something known as average rate something known as average rate

so for example you take this one you take this plot ok

so what i have here is time it can be any unit lets take it seconds

doesn't matter what i have on the y axis is concentration and what i am doing is
in this case as an example

i am looking at the change in concentration of the reactant as a function of
time right i can also

do it in ah using products but let us stick to change in concentration of the
reactant ok so

this is what happens then i will draw a line now just to show you how it changes
as a function

of time ok now there is an arbitrary reaction i am taking a very general
reaction i am not

naming the reaction as such ok it can be applicable for any general reaction
now suppose

we put our experimental points say for example as a point out here right let
there be a point

out here let there be a point out here and let there be a point out here

so the line is a smooth

line through some of these experimental points right now it is very similar if
i can ah you know

kind of take you back a couple of lectures ago it is very similar to this
kinetic reaction

profile that one is also kinetic reaction profile and you can see for these
blue

lines which corresponded to the products the reaction between hypochlorite and
bromide

giving hyper bromide and chloride how the reactants were changing as a
function of time and

this is what i am doing out here too but what are we trying to do or what am i
trying to tell you

or what am i trying to emphasize upon

so let this you know correspond to t one let this expandable

point correspond to t two is correspond to t three correspond to t four right
so let

this concentration correspond to c one c two c three and then c four

so what we have done is we

have taken a few exponential points we have labeled them correspond to

the times t one two t three t four and the corresponding concentrations at

those times c one c two c three c four now when we define the average rate when
we define

the average rate say we define the average rate between c_1 and c_3
so when we take the
average rate the average rate is defined as the average rate is defined like
this the average rate is equal to say i am taking these two points c_3 and c_1
corresponding to t_3 and t_1 .

so $c_3 - c_1$ over $t_3 - t_1$
so that is my average
rate

so if i can write here this is average rate this is equal to $c_3 - c_1$ over
 $t_3 - t_1$

i am sure you now realize there is one thing that is missing based
on our previous

discussions the rate has to be a positive quantity $c_3 - c_1$ is negative
because c_3 is less

than c_1 $t_3 - t_1$ is positive because t_3 is greater than t_1 hence this
expression is

negative because this expression is negative the rate cannot be a negative
quantity

i have a negative sign out here and again whenever you express the rate in
terms

of the disappearance of a reactant it is always preceded with a negative sign
which signifies a

it is a reactant which is disappearing with time and two the rate is a
positive quantity and that

is why this negative sign has to be there but this is not

so useful in very few cases very very few cases

you would actually see the average rate being used extensively its not
extensively

used anyway this one we can write as $-\Delta c / \Delta t$
so Δ

means a finite change in concentration over Δt a finite change in time that
means over the

time interval $t_3 - t_1$

so this is the definition of your average rate and as

i said this is not what is regularly used or is that useful what is really
useful for us is to know or is to ask if i take any time point if i

take any time point on this curve say t_1 say t_2 say t_3 say t_4 say any
other

time point will i be able to get to get the rate at that specific time
corresponding to a certain

concentration right what does this bring us to this brings us to the concept
of instantaneous

rate and that is the one we normally use throughout

so let us go and take a quick look

at what instantaneous rate is all about

so we are talking about instantaneous rate

again let us look at a similar curve right where the reactant concentration
is

decreasing as a function of time

so let me have a curve like this ok again same tables this

is concentration of reactant i say the reactant is represented

as r right this is time in this direction increasing right and my reaction

profile of the kinetic reaction profile goes like this ok and remember what we are discussing out here is something referred to as instantaneous rate now suppose these are certain time points or experimental points now suppose i want to know suppose i want to know that at this instant that means at this instant at this time point what is the rate what is the rate at this time point say which corresponds to say in this case it is t_1 say so what would i do is i would draw a tangent if i can draw it properly let me use a different color i would draw a tangent right at this point so let me just change this so i draw a tangent right at that point i draw a tangent and then what i do is i take the slope of the tangent so that means i have drawn a tangent right at t_1 right at t_1 once i have drawn the tangent right at t_1 this is what my the change in concentration of r which is d of r and along this axis i have can write the change in t which is d t so the way this instantaneous rate is different from the average rate is this when i say instantaneous rate what i am meaning is you know going back to this average rate definition where $\frac{c_3 - c_1}{t_3 - t_1}$ when i am talking about instantaneous state what i mean is i am meaning that $c_3 - c_1$ tends to 0 $t_3 - t_1$ tends to zero so this is based on the expression we had out here so there is very small difference between c_3 and c_1 essentially that means i am taking the rate at a specific point hence the rate or the instantaneous rate is defined as $\frac{d c}{d t}$ so based on this based on this what i can write is so based on this exercise what i can write is then the rate so i can write $r_{\text{instantaneous}}$ which is the instantaneous rate is equal to is equal to $\frac{d \text{ of } r}{d \text{ of } t}$ right with a negative sign before that again the negative sign has to be there because r being the reactant the rate has to be a positive one so what is the instantaneous rate giving you or what is the instantaneous rate all about the instantaneous rate is the slope of the tangent the slope of the tangent drawn at that point that point means the point where you want to find the instantaneous written ok so i will write it so that becomes clear so then the way we characterize instantaneous rate or try to find instantaneous rate is by drawing a tangent at that instant or that time point which in our discussion was t_1

so the one is number one and then once i have drawn a proper tangent

so tangent has to be done properly right once i have drawn a proper tangent then what i do is i take the slope of the tangent

so these two things i need to do to find the instantaneous rate ok

so if this is a rate or if you are looking at the rate in terms of the reactant concentration it would be minus d of

r over d of t if you are looking at the rate in terms of the product concentrations it would be d of p over d of t

so that means for products similarly i draw i will draw a tangent at that point and my r instantaneous would be d of p over d of t this time p here is product p here is product

so this is a very crucial difference between the instantaneous rate and the average rate

so the average rate is taken over a longest time interval a long change in concentration over the time interval and it

is not of that much use that's why it's not used there often the instantaneous state is typically the

one which is used throughout and that is what we saw or what we looked at how it is defined

based on this you can understand that i can have instantly address rates at typically many points

so i can have see if you if you want this point now right if you want this point what

you do is you draw a tangent at this point right now my tangent was not drawn properly or if you want to at this point you draw again a tangent at this point ok

so if you want it here then you draw a tangent at this point

so wherever at that instant you want the rate you draw the tangent at that point and then do the exercise that means take

the slope of the tangent for example here you take the slope

so from here to here what are we looking at we are looking at a change in the reactant concentration from here to here what are we looking at we are

looking at a change in time why because this is the y axis the y axis is telling you about

the concentration of the reactant this is parallel to the x axis it is telling you about the

time that is elapsed or rather the time interval $d t$ in this case

infinitesimal time interval right

and that is the definition of instantaneous rate and this instantaneous is the one

which is used almost all the time ok there is one more aspect that we have

so we have talked about average rate we have

talked about instantaneous rate a very important rate that comes in a type of rate

is referred to as initial rate that is initial rate of reaction initial rate of

reaction and how do we do that see what does initial rate of reaction mean
initial rate of reaction means that exactly at the start of the reaction i
need my rate that is the moment the reaction is started i need to calculate the rate of the reaction
see unless and until my direction has started i cannot calculate any rate or what i am saying by
initial rate is that if i have to calculate my initial rate i have to be very very close to the start
of the reaction i have to let the reaction start otherwise i cannot calculate any rate anyway
but once the reaction starts i immediately calculate reaction rate

so at the very initial point at the very first few points

so then if i have to depict it pictorially or using a kinetic reaction profile same thing if i have this for a reactant this is time this is concentration right if this is my initial time

point remember this is zero

so this is my initial time point i have to find the initial reaction rate

so what i do is what i do is i draw let me use this pen this is clearer i draw tangent

at this point i draw a tangent at this point this tangent this tangent what does

it give you it gives you the initial reaction rate from the slope of this line and the way this tangent

is drawn is it is drawn right at the initial point of the reaction now this was is you know

this was in terms of the reactant that's why you see decreasing as a function of time i can do

exactly the same thing in terms of the product

so for example if i have not done it before for the other cases but just to complete the story again this is time this is you know concentration of product this is concentration of product and i say the product reaction profile goes something like this ok

so look at the initial time point

now

so the initial time point is this this is time 0 and if i have to look or if i have to get the initial rate the initial rate or the tangent has to be drawn right at

this point and hence again this is my initial reaction there is an initial reaction rate from product right

so as usual i can get my initial

reaction rate from the reactant and i can get the initial reaction rate from product two points worth remembering one when i you know

later what i will try to do is i will give you some idea of ah you know how people would measure

rates and

so on and there is a method referred to as method of initial rates

so method of initial

rates actually takes this into consideration right you look at the initial rate and then you get

kinetics and other informations about the reaction whichever you are doing at

the time
those things will discuss in due course but there are two important points
if you are doing an experiment
so from the experimental point of view from experimental point of view there
are two key points when you
do this initial rate calculation one it is preferred it is preferred to do the
initial rate calculation based on product appearance
so that means if you are given
an option if someone asks you during calculation of the initial rate which
would
i rather choose should i go and use the reactant profile or should i go and
use the product kinetic
reaction profile your answer would be the product why this is something we
need to understand see when we are considering
the initial rate of reaction that is very logical you will see see when you
are considering the initial rate of the reaction in terms of the reactant loss
or reactant
disappearance see at this point at this point you have a huge amount of
reactant right
and then very close to that initial time point you are trying to get a measure
of
how much of reactant has been lost but do realize that if you do not
have a very sensitive technique or very sensitive analytical technique
because
you are very close to your initial time point right the difference in between
the two
concentrations that means the slope you take the difference between the two
concentrations
experimentally would be very small because this difference would be very small
if the
analytical technique is not sensitive enough then you might not get much
accuracy i repeat
when you do this initial weight calculation
so please remember this when you do this
initial weight calculation or experiment you would rather do this in terms of
the
product appearance as opposed to the reactant disappearance why when you
consider the reactant
the reactant is present say there is no product at all you are doing the
initial rate which is very
close to the starting point of the reaction you have lost only a little bit of
the reactance say
depending upon the reaction obviously and because there was a lot of reactant
to start with and you
have lost a little bit if your technique is not sensitive enough to figure out
the difference then
you will not be able to get a proper reaction rate that means your reaction
rate calculation would
not be that accurate however think about the product
so that means the rate in the reaction if
this is the initial rate you get very close to the very close to the starting
point which it should
be which you should be which is my next point for the initial rate calculation
then the difference

between the two concentrations you measure might not be high and if the technique you are using is not a very sensitive analytical technique then the change in concentration you get might not be the accurate one on the other hand think about the product appearance see look at this product appearance when starting at $t = 0$ which is my initial part even before the reaction is started on y axis we have concentration of products i have no product at all right now the moment my reaction is started a little bit of product has come in but because my initial concentration product was zero it becomes much easier for me to measure that change in concentration because i am always comparing with zero where there was nothing and i do this change with respect to zero or blank that means there was no product out there and hence i am in a much better position in terms of accurately telling or determining the product concentration and then the initial reaction rate from the product appearance and that is why the statement was made it is preferred to do the initial rate calculation based on product appearance experimentally and the second point is the second point is this initial rate calculation has to be done very close to the starting point in terms of time of the reaction it is typically you know that's what people say it is ah typically you know within five percent so understand what i am saying is where would i measure the initial reaction rate which points would i take where would i experimentally measure this is within five percent of the reaction within five percent of the reaction that means the reaction started it goes to hundred percent reaction complete within the first five percent i would have to take my concentrations for my initial rate calculation finally if you would realize from this the slope of this line and the slope of this line that for almost all reactions provided they are not chain reactions again keep this in mind provided these are not chain reactions apart from chain reactions and talking about all other reactions this initial rate the tangent or the slope of the tangent at the initial rate is always the steepest that means the slope is always the maximum that is the line is the steepest so we can write except accept chain reactions except chain reactions right the initial rate line or tangent if you would prefer to say that will be the one which is the steepest that is having the maximum slope steepest means the one which is going to have the maximum slope and that's why it is the initial rate so what did we learn from these plots we looked at three different rate definitions one was the average which was Δc over Δt then was the instantaneous by which we meant that you take any time point on that

kinetic reaction profile

if you want to know the reaction at any time point that's why it's called instantaneous rate at that instant say t_1 t_2 t_3 then what you do is you draw a tangent at that point draw the tangent properly

once you have drawn the tangent you take the slope of the tangent and that slope gives you

the instantaneous reaction rate at that instant that time part corresponding to a certain

concentration the third one is called the initial reaction rate and by definition the

initial reaction rate corresponds to that reaction rate which is measured very close

or right at the initial part of the reaction and as I said one of those two points it should

be within the five percent of a reaction whether it is in terms of reactants or products and

obviously it is preferred that instead of reactant you use the or reactant disappearance you use the

product appearance to define your initial reaction rate or find your initial reaction rate this

is something which is very important for you to understand and also take into consideration if you

are looking at a certain experiment and trying to figure out what the initial rate is this as I was

telling you this method of initial reaction rates is very important in determining the rate constant

and even the order of a reaction which you will realize when we do a few examples later now

having talked about the different types of rates that are present out there our next

approach which I will start off a little bit today unless a next approach would be to figure

out something known as rate expressions that means how is this rate related to the

concentration in some way or the other

so let's think about that for a bit

so what we do now

is we start with this concept of dependence of reaction rate on concentration and pay attention to this

so let me draw again a kinetic reaction profile for a reactant ok

so this is again concentration of reactant which

is r ok this is time as usual now let me draw the profile suppose this is a profile now let's see what is happening let us take a couple of points along this reaction profile

so let us take this point out

here which say corresponds to t_1 right and I draw I you know I am trying to find the instantaneous rate at this point take a

so if I try if I am trying to find the

instantaneous rate at this point what I would do is I would draw a tangent at that point having

said that let's look at another point out here again I need to find out the instantaneous

rate at this time point say which is t_2 i do that how as before what i will do is i will again draw tangent ok now hopefully you realize what i am getting at another time point say i take this one t_3 ok again i draw a tangent i take another time point say here corresponds to t_4 and i draw another tangent let me write these lines as a b c d e f and then g h so there are four time points at the four time points at the four time points i want to know the instantaneous reaction rates

so what have i done at all or each of these four time points i have drawn tangents so for time point t_1 my tangent is a b for time point t_2 my tangent is c d for

time point t_3 my tangent is e f for time point t_4 my tangent is g h now immediately

realize because the instantaneous rate is nothing

so instantaneous rate is what is the slope of the tangent obviously with a negative

sign right because this is a reactant we are talking about

i am not writing that its obvious what you will understand is if the slopes if you look at the slopes of the lines a b c

d e f and g h this is the order of the slope a b the slope of a b is greater than the slope

of c d which is greater than the slope of e f and which is greater than the slope of

line g h

so a b is having the maximum slope

so this guy line a b has the

maximum slope and this one has the minimum slope i just want to mention that what i

mean by the maximum slope when i say maximum slope what i actually mean is its that the magnitude of the slope is the maximum ok again what i mean my maximum

slope is

the magnitude which is i am talking about the magnitude of the slope is the maximum

and

so please remember that whenever i refer to the slope as being the maximum slope

or the minimum slope it is always the magnitude that i am referring to

so this is the one i am always i am always referring to ok

so this is something

which is very important to keep in mind in terms of the slope or slopes that we are

talking about or we are going to talk about in the later classes right you can see how

steep this one is less steep this one is lesser less steep at this one and finally this one

is the least steep or having the smallest slope what has happened what has happened is as i move

from t_1 is equal to zero along the time points t_1 t_2 t_3 and t_4 i am losing that

means reactant is disappearing that means the concentration of the reactant is changing because

of the concent because the concentration of the reactant is changing you can see the instantaneous

rate is also changing which is defined by the slope of the tangents is also changing
so that
means the rate is maximum at the time point t_1 and it is based on the example given out it
is minimum for time point t_4 the moment you see a picture like this you start thinking
this ok this is why the rate of the reaction is somehow dependent upon the concentration
of the reactant which is remaining i repeat i will stop here by this or you know making the statement since the slope is changing as a function of my time points and
since the slope is my instantaneous reaction rate that means the rate instantaneous
reaction rate is changing as a function of time what is also changing as a function of time is your concentration and if you try to merge both these observations what would immediately fall
out is that the rate is some way dependent on the concentration of the reactant that is
remaining in the mixture and maybe this is where all or this is what is the starting point
of the rate expression which is proportional to the constant of the reactant raised to
some power which we will come to know as the order of the reaction we will look at it
in more details in the next lecture thank you you