

next we are going to discuss one very important topic under colligative property that is osmotic pressure osmosis and osmotic pressure ok let us try to understand what is this osmotic pressure is let's have two bigger in this beaker i have pure solvent only pure solvent and another beaker i have solution solution and now these two beaker are connected by a tube but in between there is something called semi permeable membrane semi permeable membrane what is the semi permeable membrane it will allow the small solvent molecule to pass through but it will not allow any solute molecule to pass through so here we have pure solvent here we have a solution so this side we have ah some solute molecules so that will not go through so here it will always remain pure solvent only solution the solvent molecule can pass through from this ah semi permeable membrane and then we will see the rise there will be some ah solvent molecule passing through from this side to this side and then there will this side will go down and this thread will rise and this change in height which can be directly related to the pressure and that is called osmotic pressure ok and this again i can apply a pressure over here such that the such that the concern the height becomes same on both side that pressure has to be equal to the osmotic pressure and this osmotic pressure is experimentally verified it is equal to the osmotic pressure is equal to concentration this is molarity gas constant multiplied by temperature this is a very important quantity this is exactly used to get clean water by reverse osmosis that is if i apply pressure more than the osmotic pressure then i can send i can transfer solvent which is going to go through the semi permeable membrane to other side and this side will have only pure solvent drinkable water okay and but it has a lot of technological importance also as we have seen if i have a one more point one molal solution if i have a 0.1 molal solution then the change in boiling point is going to be Δt_b is going to be $k_b m$ and that k_b is around 0.5 so Δt_b is going to be approximately 0.05 degree centigrade very small change in boiling ah point but what about this let's see okay i can assume in this case this is a very dilute solution so 0.1 molal is approximately equal to 0.1 molar okay let us look at the definition of molality molarity is moles of solute divided by

weight of solvent what is molarity molarity the moles of solute divided by volume of the solution

so if we assume one liter solution a dilute solution has a more or less one kg of it which is a fairly good assumption for water in that case molality and

molarity is going to be same now

so 0.

1 molar at room temperature is going to be approximately 0.

1 molal is going to be approximately 0.

1 molar

so for 0.

1 molal solution ΔT the change in the boiling temperature is 0.

0.52 but in case of osmotic pressure let's calculate it

so for 0.

1 molar solution this is going to be 0.

1 multiplied by

less assume the temperature is around 0 degree centigrade

so this $R T$ is

22.

4 liter atm

so i am going to get 2.

2 atm change in pressure that is huge its easily measurable that is more than the

twice of the pressure exerted by atmosphere you see that this is a point zero five

four point one mole and this is 2.

2 atm

so this quantity this osmotic pressure becomes very important when we are trying to calculate the concentration or molecular weight of an in

a biological system where the molecules are huge very big they have a very large weight but the

concentration is quite small because the moles may be one mole might have a thousands of gram weight

so when the concentration is very very small still less concentration is like a millimole

and one is smaller we are ΔT is going to be negligible but we still can get

appreciable change in osmotic pressure and that would be very useful to calculate the

concentration or if we know the concentration then the molecular weight of these

biological proteins and things like that okay let's do an example uh 200

centimeter cube of an aqueous solution

of a protein contains 1.

2.6 gram of the protein the osmotic pressure of such a solution at 300 kelvin is found to be 2.

57 into 10^3 bar calculate the molar mass of the protein let

me read out one more time 200 centimeter cube of an aqueous solution volume is

200 centimeter cube that is 0.

2 liter contains 1.

26 gram mass of solute is 1.

26 gram of the protein the osmotic pressure of such a solution at 300 kelvin is found to be 2.

57 into 10 power minus 3 bar calculate the molar mass of the protein okay

so we are given pi this is exactly here c is a concentration okay the concentration over here

is a molar concentration

so that is defined as moles of solute divided by volume of the solution

so i am going to assume that since the concentration is going to be extremely low

so volume of the solute is equal to the volume of the solution

so we are going to get this quantity

0.

2 molecular weight n2 is simply weight of the solute 1.

26 gram divided by

um molecular weight of the solute that is the unknown quantity

so we plug in all this information and we get 1.

26 w 2 into 0.

2 is equal to r in a proper unit

so i need this

in a bar unit and that is going to be 0.

083 083 liter bar per mole per kelvin

into temperature that is 300 kelvin

so only unknown is w2

so let me rewrite it

so w 2 is going to be 1.

26 into 0.

083 into 300 divided by 0.

2 into

2.

57 into 10 power minus 3

so if i plug in all this information

i am going to get w two as sixty one thousand zero two two gram per mole ok

so this is a huge protein molecule

now i will leave it as an exercise for ah for the viewers that if i for the same

solution if i ask to ah calculate the change in freezing point and boiling point is going to

be really negligible and won't be able to we will probably measure it experimentally

okay let's do another problem at 300 kelvin 30 gram of glucose present in a liter

of its solution has an osmotic pressure of 1 4.

98 bar if the osmotic pressure of the

solution is 1.

52 bar at the same temperature what would be its concentration it at 300 kelvin

so temperature is given temperature is important for osmotic pressure at 300 kelvin 36

gram of glucose

so solid weight of solute is 36 gram is present in 1 liter
so volume

is 1 liter has automatic pressure of 4.
98 bar if the osmotic pressure of
the solution is 1.

52 bar then what is its concentration ok
so in

this equation π is equal to $c r t$

so four point nine bar is equal to c is 36 gram divided
by molecular weight of glucose that is $C_6H_{12}O_6$

so 72 plus 12 plus 96

so 6×10^{-3} in

1 liter $r t$ now is asking if 1.

52 bar is osmotic pressure then what

is concentration ok looks like this information has no value not required
so c is simply given by 1.

52 divided by θ .

0.83 into 300 kelvin and the answer would come out to be divided by
point zero eight three divided by three hundred point zero six point zero six
one molar ok

lets discuss now ah abnormal molar masses ok

so we have seen using the colligative

properties we can calculate ah molar mass for example using Δt of boiling
using

this equation we have calculated molar mass of solute but we have been talking
about

non-ionic solute what about ionic solute what happens if ah solute goes into
the solution

and it might dimerize or it might dissociate for example if i take $NaCl$ put it
in a water is going

to dissociate to n a plus request plus $c \times 1$ minus x if i took point molal
solution to begin

with invert in water then this being a very strong electrolyte it's pretty
much going to

less assume it's going to dissociate completely and we are going to get θ .
1 molal and a plus

and θ .

1 molal Cl^- minus and nothing will left so that's the assumption fairly good
one okay and we

know the colligative property doesn't depend upon what solute you are using it
depends on

simply the concentration of each and in every individual ah solute added up
so to calculate

qualitative properties now we have zero point one molar and applied zero point
one molar Cl^-

minus and total concentration which is going to go into this equation is going
to be θ .

2 molar

if for example it dissociate only 50 percent we know it's not going to
dissociate it is going to

dissolve much more but let us assume that is going to dissociate only fifty
percent then out of zero

point one mole $NaCl$ what is left is zero point zero point zero five molar $NaCl$
and remaining will

convert into $n + c(1 - \alpha)$.

0.5 and 0.

0.5

so the total concentration molarity which is going to get into this equation is going to be you add these three individual quantities

so in solution

initial is present any plus is present $c(1 - \alpha)$ is present

so for this equation it doesn't matter

what is present you just want the concentration of all the solute present

so the total concentration

is now going to be not 0.

1 molal but 0.

15 mole if we can define the degree of dissociation for

example if a degree of dissociation is α then 0.

1 into $1 - \alpha$ will remain in the

solution and rest will convert into in this $n + c(1 - \alpha)$ that would be 0.

1 α and 0.

1 1

so the total concentration is going to be simply add up these three quantities and that will go to this and using if I know

ΔT if I know K_b and if I know how much NaCl I added to begin with I can calculate degree

of dissociation that is a very important quantity not only dissociation sometimes we

can have a dimerization we have some compound which put in the solution at my

diameters it might polymerize polymerizable so in that case if I start with concentration

of n and degree of polymerization is α then what is left is $n(1 - \alpha)$

and how much a_2 we are going to get is

so out of n moles $n\alpha$ moles has

converted to a_2 and giving rise to $n\alpha$ by 2 moles of a_2 .

so so when calculating

the total concentration the amount the moles which is going to go into the calculation is this plus

this

so in this case the concentration has gone down for example now if I have a general $a_m b_n$ compound let's say $a_m b_n$ the concentration is c degree of dissociation is $1 - \alpha$ sorry degree of dissociation α then this compound which will remain in the solution is this much and we are going to get a ion that

the concentration of that ion is going to be $c\alpha m$ and the concentration of b ion is going to be $c\alpha n$

so the total concentration is going

to be this plus this plus this okay let's do some exercise to understand this concept

so this is the example 2.

12 let me read 2 gram of benzoic acid is dissolved in

25 gram of benzene

so is a depression and freezing point equal to 1.
 62 kelvin molar depression constant of benzene is 4.
 9 kelvin kg per mole what is the percentage association of acid if it forms dimer in solution okay
 so we are given 2 gram of benzoic acid
 so that is solute
 so weight of solute is 2 gram benzoic acid that is C_6H_5COOH dissolved in 25 gram of benzene
 so that is solvent
 so it dissolving 25 gram of benzene
 so the depression in freezing point equal to 1.
 62 kelvin
 so ΔT is 1.
 62 kelp molar depression constant for benzene is constant is K_f is 4.
 9 kelvin kg per mole what is the percentage dissociation of acid if it forms dimer solution
 so this benzoic acid in the solution is going to give me C_6H_5COOH twice of that and not all of it is going to be damn rice is asking what percentage is going to have or and percentage association okay
 so percentage is asking okay
 so we will start with our familiar equation so that is ΔT is equal this is to freezing point so depression so this is $K_f m$ K_f is given right here and we need the molality of all the species present the species which are present is C_6H_5COOH and its dimer benzoic acid and its dimer so we started with 2 gram to calculate the molality we need to convert this 2 gram to moles of benzoic acid so we need the molecular weight so molecular weight is going to be ah say one carbon so that is 84 690 plus 32 so twenty two so we get ah moles of benzene acid as two dividers one twenty two and then we are going to have a some diagonalization so present diagonalization let's say the degree of dimension is alpha so we are going to get 1 minus alpha and we are going to get this dimerization 2 by 122 alpha that many benzoic acid dimerized and the concentration of the due to dimer is going to be half of that so the total concentration is going to be this plus this okay i'm sorry we need to still need to calculate the concern the number of moles of benzoic acid present in the solution is

going to be this and
 moles of diameter present in the solution is going to be this
 so we are given weight of the solvent
 so the molality the total molality of both the species both the solute is
 going to be just
 added up
 so we are going to get 2 divided by $1 - 2\alpha + \alpha^2$
 by two
 so this is the moles divided by twenty five gram and that we need
 to convert into kg
 so just multiply with also zero point zero point six six one minus alpha by two
 so
 that is going to be the molarity
 so now we have all the information we need to just calculate
 alpha and just multiply by 100 that will give me an percentage association so
 $\Delta T_f = 1.62$ kelvin equal to $4.9 - 0.661\alpha$
 $1.62 = 4.9 - 0.661\alpha$

so we are going to get $1 - \alpha$ by 2 as 1.62
 1.62 divided by 4.9
 9 divided by 0.66
 0.500
 so alpha by two is going to be point five zero zero
 so alpha is going to
 be one
 so this is a nearly hundred percent association
 so nothing will remain practically
 nothing will remain of this everything will convert into diamond if i put
 benzoic acid
 in benzene okay let's do another problem the next exercise okay let me read it
 out
 0.6 meter of acetic acid having density 1.06 gram per meter is dissolved in one
 liter of water the depression in freezing point observed of this strength of
 estimate
 0.205 degree centigrade calculate the van't Hoff factor and the dissociation
 constant of s okay
 let me first define what is one van't Hoff factor is
 so one van't Hoff factor is concentration of the species present in
 the solution let me call that experimental concentration and divide by
 theoretical
 concentration theoretical concentration is the concentration which i am
 calculating
 that is the concentration before any reaction happens in the in the solution
 that is
 any dissociation or polymerization happens
 so that is the concentration
 theoretical concentration ok and this this concentration can be in
 a molality it could be in an and molarity whichever one

so if i am trying to calculate say automatic pressure p_i is equal to $c r t$
 so if i substitute c as a theoretical then p_i is the going to the calculated one and if i substitute c as the experimental the actual concentration present in the solution then it will be experimental one
 so it's clear to see that this is basically going to be p_i experimental by p_i vertical or if i am calculating let's say freezing point depression or boiling point ΔT then ΔT is again k_b by m this is a molarity and again we are going to get
 so if i substitute theoretical concentration then i am going to get what ΔT i calculate by putting the concentration which i am using or experimental would be or the concern ΔT experimental change in temperature would be ΔT using the molarity of the ΔT component present in the solution
 so again we can substitute ΔT concentration equal to ΔT by k_b k_b will cancel out in both ways and again i will get ΔT experimental and ΔT calculated or theoretical
 so you can see one τ factor is simply experimental qualitative properties experimental qualitative properties divided by calculated calculated calculated colligative properties so that is how the one top factor is defined
 so for example if $NaCl$ is going to dissociate completely then one $NaCl$ is going to give me two ΔT species one n_a plus and another c
 1 minus
 so my ΔT experimental concentration would be twice of theoretical concentration so one top factor in case of $NaCl$ is going to be two if is going to dissociate completely ok so the problem which we are going to attempt is asking for to calculate one top factor okay
 so in this problem we are given ΔT .
 6 meter of acetic acid liter of acetic acid having density it dissolved in one liter of water
 so volume of solvent is one liter the depression and freezing point ΔT_f was observed to be zero point zero two zero five degree centigrade
 calculate the want of factor
 so we need to calculate i and dissociation constant for the ΔT ok
 so dissociation constant of k_b is defined as follows
 so first let me write the reaction acetic acid that is CH_3COOH when it goes into water it is dissociates and gives me acetate ion and H^+ plus of course it is a acid it has to give H^+ plus okay and
 so the k_b is defined as concentration of H^+ plus concentration of acidic ion divided by concentration of CH_3COOH and the

concentration unit which is used here is molarity okay and we need to you use this equation also that is defined as k_f multiplied by m so this is molality so but in this problem we are going to consider molarity and molarity happen to be same why is that we are going to consider that one liters water is equal to one kg of water and if i add 0.6 ml of acetic acid it is not going to change the volume of solution so we are going to assume 1 liter of water is equal to 1 kg of solvent and that is equal to 1 liter of solution so if i am going to calculate the concentration that would be moles of solute so that is weight of solid that we can calculate by volume of solute multiplied by density so the weight of solute is 0.6 into 1.06 divided by ah this is the weight of solute and we if we divide by molecular weight of solute that would be 12 or 24 plus 4. 38 plus 32 12 15 20 60 60 so weight of solute divided molecular weight that is moles of solute divided by weight of solvent since we are assuming 1 liter water is equal to 1 kg of water so we can divide by 1 kg so this will give me molality and if i want to calculate molarity i again have assumed that 1 kg of water or 1 liter of solvent if i add solute to it is not going to change its volume so instead of one carry i use one liter and i again get the same answer it's simply 0.6 into 1.06 divided by 60 i can either molarity or molar d it's a same number so so i am going to get 1.06 into 10 power minus 2 molar or molar it doesn't matter so we have calculated the concentration if degree of dissociation is alpha then if the initial concentration was c which is right here and degree of dissociation is alpha then c multiplied by $1 - \alpha$ that much acetic acid will remain in the solution and remaining part will convert dissociate and is going to give me $c \alpha$ of acetate ion and $c \alpha$ plus n then if i take that all that information and put it right here i'm going to get $c \alpha^2$ divided by $c (1 - \alpha)$ ok and where c is given right here ok so we need to calculate k_b we need to calculate i so now the total concentration which i am going to use while calculating the colligative property that is going to be concentration of all the

individual
 ah component in the solid
 so these all these three are solute in the solution
 so the
 total concentration is simply going to be this plus this plus this and that is
 going to be c_1
 plus α ok
 so i have now all the information i just need to calculate α since i know
 c
 if i know the α then i can calculate the k_b and of course i can calculate
 i also
 on the one top factor and that would be the experimental concentration that is
 this
 concentration that is after dissociation and the concentration before
 dissociation
 that is c
 so it's simply one plus α
 so i just need to calculate α and i will
 have all the ah answer i require okay
 so i am just going to plug in all the information in
 this equation
 so for this i of course need k_f and k_f is given in the table and if i take
 it
 from there it is 1.
 $86 \text{ ah kelvin kg per mole } 1.$
 86 and the molality is you already defined c that is one point zero six into
 ten
 power minus two multiply one plus α and now i can calculate one plus α
 that is going to be point zero two zero five
 divided by one point eight six divided by point zero one zero six and answer
 is one point zero three nine seven or one
 point zero four one point zero three nine seven
 so α is going to be
 point zero three nine seven
 so one top factor we have already calculated
 that is one point zero three nine seven now what about k_b
 so if i put all this information 1.
 0 into 10 minus 2 α square that is 0.
 0397 square divided by 1 minus α
 so 1 minus 0.
 0397 let's see what answer we got
 so okay the answer which we are going
 to get is 1.
 74 into 10 power minus 5
 so within round of error
 this is i think is the answer okay let's discuss one more problem from the
 text this is 3.
 32 from insert ebook calculate the depression in the freezing point of water
 when
 10 gram of $\text{CH}_3\text{CH}_2\text{CHCl}_3$ is added to 250 gram of water
 so he's asking calculate the depression
 and freezing point
 so he's asking ΔT_f ah when 10 gram
 so weight of solute it and

tandrum and the solute is $\text{CH}_3\text{CH}_2\text{CHClCOOH}$

so 10 gram of this is added to 250 gram of water

so weight of solvent is 250 gram and we are given K_a is equal to dissociation constant for

this acid is 1.

4 into 10 power minus 3 and K_f for water is 1.

86 kelvin kg per mole ok

so we need to calculate depression and freezing

point the usual formula is going to be $\Delta T_b = i K_b m$ and where the molarity of all the component

present ok just for the simplicity let me write this as a

so this whole compound is simply H^+

which is going to dissociate and going to give me H^+ plus plus a minus in solution and again if the

concentration the theoretical concentration is c of H^+ then after dissociation if

the degree of dissociation is α then after dissociation the concentration of

H^+ will become c multiplied by $1 - \alpha$ concentration of H^+ plus will become $c\alpha$ and

concentration of A^- will become $c\alpha$

so now i can write K_a which is defined as

concentration of H^+ plus multiply the concentration of A^- divided by concentration of HA

we can write this in terms of c and α so concentration of H^+ plus $c\alpha$ consider a minus c

α and concentration of H^+ is $c(1 - \alpha)$

so putting it and removing one c we are going

to get $c\alpha^2$ divided by $1 - \alpha$ ok now let us try to calculate c that is the concentration of the solute in the solution

before dissociation

so c is if we want to write in molarity

then it is going to be moles of solute divided by weight of solvent in kg but we are going to consider the molality and molarity to be same because

we are going to assume the weight of solute weight of solvent is 0.

250 gram and the volume of

the solution is also 0.

250 liter

so in that case the concentration in terms of molality or molarity

is going to be same to calculate the concentration we need a molecular weight of this compound and so

the molecular weight of this compound is going to be 15 plus 14 plus 13 plus 35.

5 this is 12 plus

113 plus 30 to 45

so this would be 35 plus 45 80 80 plus 1529 plus 13 42 and 0.

5

so this is 122.

5

so molecular weight of this compound is 122.

5

so moles of solute and 2 is simply 10 by 122.

5

so i have all the information now to calculate

c

so this would be \tan divided by 122.

5 divided by weight of solvent that is 0.

250 kg

so kg and if i just evaluate this 0.

3265 point three two six and now i need alpha to cal

so this information i am going

to put it in this equation

so i will get point three two six alpha square divided by one minus

so this is to solve quadratic equation but let's see if we can make

approximation less first make

approximation alpha is negligible with respect to one in that case alpha is simply ah 1.

4 into 10

minus 3 divided by 0.

326 and square root of that

so the answer is alpha is equal to point zero six five five

so we

ignored point zero six five five with respect to alpha

so if you want to refine the solution

we are just going to substitute this alpha in the denominator recalcuator but this is

a very nice method to if you don't want to solve this quadratic equation or if some

cases even higher order equation i can do it iteratively just make

approximation over here

calculate alpha and whatever alpha you get just keep on substituting and

couple of iteration most

probably it will converge many times diverge also but i've seen most of the time it converge so

just replacing back this

so i'm going to get k_a is equal to 0.

326 alpha square divided

by 1 minus alpha that would be 0.

9345 and now using this equation where

k is given here i will get 63

so alpha is simply point zero six

three three

so it's quite close all right

so we have calculated alpha

now we need to calculate delta t where m is going to be the total concentration of all

the species in all the species which are present is $h_a h$ plus a minus

so if i add up the

concentration the m is simply going to be c multiply 1 plus alpha

so if i put all the

information here k_b is given i am sorry this is k_f k_f is given is 1.

86 multiplied by c which is i

we have already calculated somewhere that is 0.

326 multiplied by one plus alpha alpha is point

zero six is one plus alpha one point zero six three three and now we can calculate delta t f is going to be 1.

86 multiplied by 0.

326 multiplied by 1.

0.633 and answer is 0.

645

so change in freezing point is going to be 0.

645 degree centigrade or degree kelvin if one want to calculate an one top factor then we that also

we know it's simply one plus alpha

so one top factor is one plus alpha which we have discussed in the last class and that is equal to one point zero six three three ok

let us try to solve one last problem in this session okay the next problem nineteen

point five gram of CH_2FCOOH is dissolved in 500 gram of water the depression and

freezing point of water observed is 1.

0 degree centigrade calculate the want of factor

and dissociation constant of fluoroacetic acid okay this is a very ah this is quite similar

to the problem which we have discussed earlier okay

so 19.

5 gram of this acid

so weight of solute

is 19.

5 gram and the solute is CH_2FCOOH dissolve in 500 gram of water

so weight of solvent is 500 gram depression and freezing point is water is observed to be 1.

0 degree centigrade

so ΔT_f which is observed is one point zero

degree centigrade calculate one top factor i and the dissociation constant K_a ok again if i write this whole equation

dissociation of HA giving me H^+ plus A^- a minus where i am assuming this is a then if initial concentration is c undissociated concentration and after dissociation

degree concentration is going to be one minus α then the concentration of H^+ plus is

going to be $c - 1$ for concentration is here so

so total concentration of each and every

species is going to be $c - 1 + \alpha$ so one top factor as we have already discussed

is going to be $c - 1 + \alpha$ divided by c that is 1 and K_a is going to be

concentration of H^+ multiplied by concentration of A^- divided by concentration of HA that is $c - 1 - \alpha$

so that would be $\alpha^2 / (c - 1 - \alpha)$ okay and we can calculate c

so c is going to be

molarity or molarity again we are in this dilute aqueous solution molarity and molarity

we are going to assume it to be same so we are given mass and we want to convert it to

moles

so to convert to moles we need a molecular weight again molecular weight of this compound

is going to be 14 plus 9 plus 12 plus 13 plus 30 plus 45

so 49.12378.

so molecular

weight is 78

so the concentration is moles of solute

so that would be 19.

5 gram

divided by uh molecular weight that is 78 divided by either volume of the solution which

we have considering equal to the volume of solvent or weight of the solvent

so that is to

calculate molality

so we that is 0.

5

so this is 19.

5 divided by 78 into point five point five

something

so this is oh this comes out to be one by two

so simply zero point five molal or

molar ok

so we have c and we already given t_f

so Δt_f is $k_f m$ where m is the total concentration of

concentration all the species that is c multiply 1 plus alpha

so this is

going to be k_f into c 1 plus alpha k_f is given the last problem itself so

we can use it point eight six one point eight six multiplied by point

five ah multiplied by one plus 1 okay

so we can calculate 1 plus alpha

equal to 1.

0 divided by 1.

86 into 0.

5

so 2 divided by 1.

86 okay the problem in these questions in this exercise is how many

significant

figures to carry

so okay let me carry just 1.

075 ah as one plus alpha

so alpha is becomes

simply point zero seven five if i carry just two significant i will not get an any answer

so alpha point zero seven five

so we already

have the one top factor is simply 1.

075 and K_a now it's straightforward c is we

have already calculated that is point five into point zero seven five square

divided by one minus alpha that would be point nine two five and now we can

calculate

this trivially zero seven five square

so three point 0 into 10 minus 3

so that is what we get

the dissociation constant for this acid okay

so that's where we will stop this session you