

Exemplar Problem

Conic Section

16. Find the coordinates of a point on the parabola $y^2 = 8x$ whose focal distance is 4.

Ans:

Given

Equation of the parabola $y^2 = 8x$

Focal distance = 4.

$$y^2 = 8x \text{ (given)}$$

On comparing the given equation of parabola with $y^2 = 4ax$, we get

$$8x = 4ax$$

$$a = 2$$

$$\therefore \text{Focal distance} = |x + a| = 4$$

$$\Rightarrow |x + 2| = 4$$

$$\Rightarrow x + 2 = \pm 4$$

$$\Rightarrow x = 2, -6$$

But $x \neq -6$ (because the given parabola lies in the positive x -axis direction).

$$\text{For } x = 2, y^2 = 8 \times 2$$

$$\therefore y^2 = 16$$

$$\Rightarrow y = \pm 4$$

So, the points are $(2, 4)$ and $(2, -4)$