Trigonometric Functions - Class XI

Related Questions with Solutions

Questions

Ouetion: 01

If $\sin\alpha = A\sin(\alpha+\beta), A\neq 0$ Which of the following is not the value of $\tan(\alpha+\beta)$? A. $\frac{\sin\beta}{\cos\beta - A}$ B. $\frac{\sin\alpha\cos\alpha}{A\cos\beta - \sin^2\alpha}$ C. $\frac{\sin\alpha\cos\alpha}{A\cos\beta + \sin^2\alpha}$ D. $\frac{\sin\beta}{\cos\beta + A}$

Solutions

Solution: 01

$$\frac{\tan(\alpha + \beta)}{\tan(\alpha + \beta)} = \frac{\tan \alpha + \tan \beta}{1 - \tan \alpha \tan \beta} = \frac{\frac{A \sin \beta}{1 - A \cos \beta} + \frac{\sin \beta}{\cos \beta}}{1 - \frac{A \sin \beta \sin \beta}{(1 - A \cos \beta) \cos \beta}} [From [ii]]$$

$$= \frac{A \sin \beta \cos \beta + \sin \beta - A \sin \beta \cos \beta}{\cos \beta - A \cos^2 \beta - A \sin^2 \beta}$$

$$= \frac{\sin \beta}{\cos \beta - A}$$

$$Also, \tan(\alpha + \beta)$$

$$= \frac{\tan \alpha + \tan \beta}{1 - \tan \alpha \tan \beta} = \frac{\frac{\sin \alpha}{\cos \alpha} + \frac{\sin \alpha(1 - A \cos \beta)}{A \cos \alpha \cos \beta}}{1 - \frac{\sin^2 \alpha(1 - A \cos \beta)}{A \cos^2 \alpha \cos \beta}}$$

$$[From (iii)]$$

$$= \frac{[A \sin \alpha \cos \beta + \sin \alpha - A \sin \alpha \cos \beta] \cos \alpha}{A \cos^2 \alpha \cos \beta - \sin^2 \alpha + A \sin^2 \alpha \cos \beta} = \frac{\sin \alpha \cos \alpha}{A \cos \beta - \sin^2 \alpha}$$

Correct Options

Answer:01

Correct Options: C, D