

Matrices and Determinants - Class XII

Related Questions with Solutions

Questions

Question: 01

Which of the following values of α satisfy the equation

$$\begin{vmatrix} (1 + \alpha)^2 & (1 + 2\alpha)^2 & (1 + 3\alpha)^2 \\ (2 + \alpha)^2 & (2 + 2\alpha)^2 & (2 + 3\alpha)^2 \\ (3 + \alpha)^2 & (3 + 2\alpha)^2 & (3 + 3\alpha)^2 \end{vmatrix} = -648\alpha ?$$

- A. -4
- B. 9
- C. -9
- D. 4

Solutions

Solution: 01

$$\begin{vmatrix} (1 + \alpha)^2 & (1 + 2\alpha)^2 & (1 + 3\alpha)^2 \\ (2 + \alpha)^2 & (2 + 2\alpha)^2 & (2 + 3\alpha)^2 \\ (3 + \alpha)^2 & (3 + 2\alpha)^2 & (3 + 3\alpha)^2 \end{vmatrix} \begin{array}{l} R_2 \rightarrow R_2 - R_1 \\ R_3 \rightarrow R_3 - R_1 \end{array} \begin{array}{l} \text{[Take common]} \\ \end{array}$$
$$2 \begin{vmatrix} (1 + \alpha)^2 & (1 + 2\alpha)^2 & (1 + 3\alpha)^2 \\ 3 + 2\alpha & (3 + 4\alpha) & (3 + 6\alpha) \\ (4 + 2\alpha) & (4 + 4\alpha) & (4 + 6\alpha) \end{vmatrix}$$
$$R_3 \rightarrow R_3 - R_2 \begin{vmatrix} (1 + \alpha)^2 & (1 + 2\alpha)^2 & (1 + 3\alpha)^2 \\ 3 + 2\alpha & 3 + 4\alpha & 3 + 6\alpha \\ 1 & 1 & 1 \end{vmatrix} \begin{array}{l} C_2 \rightarrow C_2 - C_1 \\ C_3 \rightarrow C_3 - C_1 \end{array} \begin{array}{l} \text{[Take common]} \\ \end{array}$$
$$\therefore 2\alpha^2 \cdot \alpha \begin{vmatrix} (1 + \alpha)^2 & (2 + 3\alpha) & (2 + 4\alpha) \\ 3 + 2\alpha & 2 & 2 \\ 1 & 0 & 0 \end{vmatrix}$$
$$4\alpha^2 | -2\alpha | = -8\alpha^3 = -648\alpha$$
$$\alpha = 0, \alpha^2 = 81, \alpha = \pm 9$$

Correct Options

Answer:01

Correct Options: B, C