

Matrices and Determinants - Class XII

Related Questions with Solutions

Questions

Question: 01

Let A and B be two symmetric matrices of order 3.

Statement-1 : $A(BA)$ and $(AB)A$ are symmetric matrices.

Statement-2 : AB is symmetric matrix if matrix multiplication of A with B is commutative.

- A. Statement-1 is true, Statement-2 is false.
B. Statement-1 is false, Statement-2 is true.
C. Statement-1 is true, Statement-2 is true; Statement-2 is a correct explanation for Statement-1.
D. Statement-1 is true, Statement-2 is true; Statement-2 is not a correct explanation for Statement-1.
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Solutions

Solution: 01

Let $A(BA) = P$

$$\begin{aligned} \text{Then } P^T &= (ABA)^T = A^T B^T A^T \\ &= ABA = P \end{aligned}$$

Thus, P is symmetric.

Also, $A[BA] = [AB]A$ by associativity.

\Rightarrow Statement - 1 is true.

Now, $(AB)^T = B^T A^T = BA = AB$ if the matrices A and B commute.

\Rightarrow Statement-2 is also true.

Correct Options

Answer:01

Correct Options: D