For three events A, B and C, P (Exactly one of A or B occurs) = P (Exactly one of B or C occurs) = P (Exactly one of C or A occurs) = $\dfrac{1}{4}$ and P (All the three events occur simultaneously) = $\dfrac{1}{16}$. Then the probability that at least one of the events occurs, is.

A $\quad \dfrac{7}{32}$

B $\quad \dfrac{7}{16}$

C $\quad \dfrac{7}{64}$

D $\quad \dfrac{3}{16}$

Correct option is B)

P (exactly one of A or B)$= P(A \cup B) - P(A \cap B) = \dfrac{1}{4} = P(A) + P(B) - 2P(A \cap B)$

P (exactly one of C or B)$= P(C \cup B) - P(C \cap B) = \dfrac{1}{4} = P(C) + P(B) - 2P(C \cap B)$

P (exactly one of A or C)$= P(A \cup C) - P(A \cap C) = \dfrac{1}{4} = P(A) + P(C) - 2P(A \cap C)$

Adding all

$$2P(A) + 2P(B) + 2P(c) - 2P(A \cap B) - 2P(A \cap C) - 2P(B \cap C) = \dfrac{3}{4}$$

$$P(A) + P(B) + P(c) - P(A \cap B) - P(A \cap C) - P(B \cap C) = \dfrac{3}{8}$$

$$P(A \cup B \cup C) = P(A) + P(B) + P(C) - P(A \cap B) - P(A \cap C) - P(B \cap C) +$$
$$P(A \cap B \cap C)$$

$$= \dfrac{3}{8} + \dfrac{1}{16} = \dfrac{7}{16}$$