

Let U_1 and U_2 be two urns such that U_1 contains 3 white and 2 red balls, and U_2 contains only 1 white ball. A fair coin is tossed. If head appears then 1 ball is drawn at random from U_1 and put into U_2 . However, if tail appears then 2 balls are drawn at random from U_1 and put into U_2 . Now 1 ball is drawn at random from U_2 .

Given that the drawn ball from U_1 is white, the probability that head appeared on the coin is-

A $\frac{17}{23}$

B $\frac{11}{23}$

C $\frac{15}{23}$

D $\frac{12}{23}$

Use Baye's theorem

Required probability = $P(H/W)$

$$= [P(W|H) \times P(H)] / [P(W/T) \cdot P(T) + P(W/H) \cdot P(H)]$$

$$= \frac{1}{2} \left(\frac{3}{5} \times 1 + \frac{2}{5} \times \frac{1}{2} \right) / \left(\frac{23}{30} \right)$$

$$= \frac{12}{23}$$

Hence option (d) is the answer.