

Four persons independently solve a certain problem correctly with probabilities $\frac{1}{2}$, $\frac{3}{4}$, $\frac{1}{4}$, $\frac{1}{8}$.
Then the probability that the problem is solved correctly by at least one of them is

A $\frac{235}{256}$

B $\frac{21}{256}$

C $\frac{3}{256}$

D $\frac{253}{256}$

Correct option is A)

$$P(A) = 1/2 \Rightarrow P(\bar{A}) = 1/2$$

$$P(B) = 3/4 \Rightarrow P(\bar{B}) = 1/4$$

$$P(C) = 1/4 \Rightarrow P(\bar{C}) = 3/4$$

$$P(D) = 1/8 \Rightarrow P(\bar{D}) = 7/8$$

$P(\text{at least one of them solves correctly}) = 1 - P(\text{none of them solves correctly})$

$$= 1 - \left(\frac{1}{2} \times \frac{1}{4} \times \frac{3}{4} \times \frac{7}{8}\right) = \frac{235}{256}$$