

Three Dimensional Geometry - Class XII

Past Year JEE Questions

Questions

Question: 01

The distance of the point $(1, 3, -7)$ from the plane passing through the point $(1, -1, -1)$, having normal perpendicular to both the lines

$$\frac{x-1}{1} = \frac{y+2}{-2} = \frac{z-4}{3}$$

and

$$\frac{x-2}{-2} = \frac{y+1}{-1} = \frac{z+1}{-1}$$

- A. $\frac{10}{\sqrt{83}}$
B. $\frac{5}{\sqrt{83}}$
C. $\frac{10}{\sqrt{74}}$
D. $\frac{20}{\sqrt{74}}$

Solutions

Solution: 01

Explanation

Let the plane be

$$a(x - 1) + b(y + 1) + c(z + 1) = 0$$

Normal vector

$$\begin{vmatrix} \hat{i} & \hat{j} & \hat{k} \\ 1 & -2 & 3 \\ 2 & -1 & -1 \end{vmatrix} = 5\hat{i} + 7\hat{j} + 3\hat{k}$$

$$\text{So plane is } 5(x - 1) + 7(y + 1) + 3(z + 1) = 0$$

$$\Rightarrow 5x + 7y + 3z + 5 = 0$$

Distance of point $(1, 3, -7)$ from the plane is

$$\frac{5+21-21+5}{\sqrt{25+49+9}} = \frac{10}{\sqrt{83}}$$