

Differentiability - Class XII

Related Questions with Solutions

Questions

Question: 01

$f(x) = |x[x]|$ in $-1 \leq x \leq 2$, where $[x]$ is greatest integer $\leq x$ then $f(x)$ is

- A. continuous at $x = 0$
- B. discontinuous $x = 0$
- C. not differentiable at $x = 2$
- D. differentiable at $x = 2$

Solutions

Solution: 01

$$f(x) = |x[x]|, -1 \leq x \leq 2$$

$$= \begin{cases} -x, & -1 \leq x < 0 \\ 0, & 0 \leq x < 1 \\ x, & 1 \leq x < 2 \\ 4, & x = 2 \end{cases}$$

$f[0] = 0$, $f[0^-] = 0$, $f[0^+] = 0$. So, $f[x]$ is continuous at $x = 0$

$f[2] = 4$, $f[2^-] = 2$ So, $f[x]$ is neither differentiable nor continuous at $x = 2$

Correct Options

Answer:01

Correct Options: A, C