

Exemplar Problems

Derivatives

26.

$$\frac{8^x}{x^8}$$

Solution:

$$\text{Let } y = \frac{8^x}{x^8}$$

$$\text{Taking log on both sides, we get } \log y = \log \frac{8^x}{x^8}$$

$$\Rightarrow \log y = \log 8^x - \log x^8 \Rightarrow \log y = x \log 8 - 8 \log x$$

Differentiating both sides w.r.t. x

$$\frac{1}{y} \cdot \frac{dy}{dx} = \log 8 \cdot 1 - \frac{8}{x} \Rightarrow \frac{dy}{dx} = y \left[\log 8 - \frac{8}{x} \right]$$

$$\text{Thus, } \frac{dy}{dx} = \frac{8^x}{x^8} \left[\log 8 - \frac{8}{x} \right]$$