

Linear Programming - Class XII

Past Year JEE Questions

Questions

Question: 01

The number of elements in the set $\{x \in \mathbb{R} : (|x| - 3) |x + 4| = 6\}$ is equal to :

- A. 4
- B. 2
- C. 3
- D. 1

Solutions

Solution: 01

Explanation

Case 1 :

$$x \leq -4$$

$$(-x - 3)(-x - 4) = 6$$

$$\Rightarrow (x + 3)(x + 4) = 6$$

$$\Rightarrow x^2 + 7x + 6 = 0$$

$$\Rightarrow x = -1 \text{ or } -6$$

$$\text{but } x \leq -4$$

$$x = -6$$

Case 2 :

$$x \in (-4, 0)$$

$$(-x - 3)(x + 4) = 6$$

$$\Rightarrow -x^2 - 7x - 12 - 6 = 0$$

$$\Rightarrow x^2 + 7x + 18 = 0$$

$$D < 0 \text{ No solution}$$

Case 3 :

$$x \geq 0$$

$$(x - 3)(x + 4) = 6$$

$$\Rightarrow x^2 + x - 12 - 6 = 0$$

$$\Rightarrow x^2 + x - 18 = 0$$

$$x = \frac{-1 \pm \sqrt{1+72}}{2}$$

$$\therefore x = \frac{\sqrt{73}-1}{2} \text{ only}$$