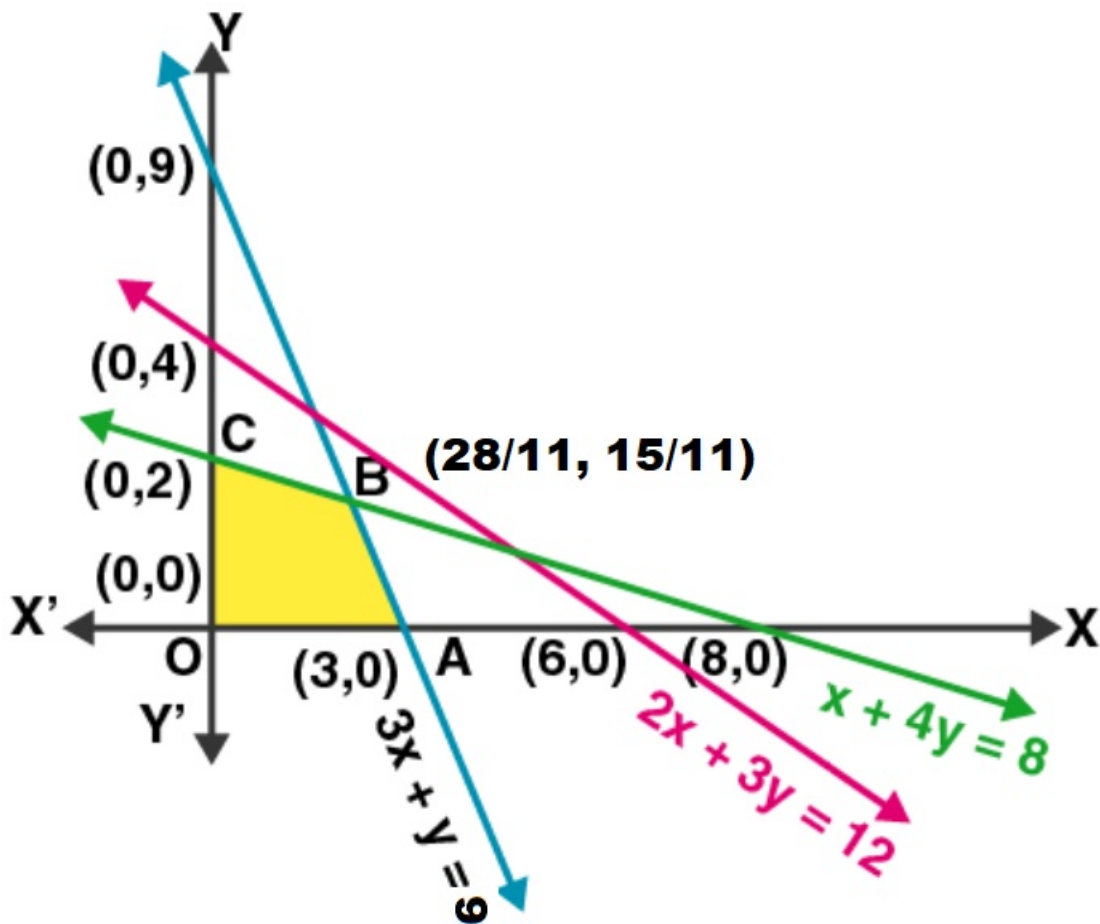


Exemplar Problems Linear Programming

21. Maximize $Z = x + y$ subject to
 $x + 4y \leq 8$, $2x + 3y \leq 12$, $3x + y \leq 9$, $x \geq 0$, $y \geq 0$.

Solution:



Given: $Z = x + y$ subject to constraints, $x + 4y \leq 8$, $2x + 3y \leq 12$, $3x + y \leq 9$, $x \geq 0$, $y \geq 0$

Constructing a constrain table for the above, we have

Table for $x + 4y = 8$

x	0	8
y	2	0

Table for $2x + 3y = 12$

x	0	6
y	4	0

Table for $3x + y = 9$

x	0	3
y	9	0

x	3	0
y	0	9

On solving equations $x + 4y \leq 8$ and $3x + y \leq 9$, we get

$$x = 28/11 \text{ and } y = 15/11$$

Here, it's seen that OABC is the feasible region whose corner points are O(0, 0), A(3, 0), B(28/11, 15/11) and C(0, 2).

Now, let's evaluate the value of Z

Corner points	Value of $Z = x + y$
O(0, 0)	$Z = 0 + 0 = 0$
A(3, 0)	$Z = 3 + 0 = 3$
B(28/11, 15/11)	$Z = 28/11 + 15/11 = 43/11 = 3.9$
C(0, 2)	$Z = 0 + 2 = 2$

From the above table it's noticed that the maximum value of Z is 3.9

Therefore, the maximum value of Z is 3.9 at (28/11, 15/11).