

Exemplar Problems

Linear Programming

14. A company manufactures two types of sweaters: type A and type B. It costs Rs 360 to make a type A sweater and Rs 120 to make a type B sweater. The company can make at most 300 sweaters and spend at most Rs 72000 a day. The number of sweaters of type B cannot exceed the number of sweaters of type A by more than 100. The company makes a profit of Rs 200 for each sweater of type A and Rs 120 for every sweater of type B.

Formulate this problem as a LPP to maximize the profit to the company.

Solution:

Let's assume x and y to be the number of sweaters of type A and type B respectively.

From the question, the following constraints are:

$$360x + 120y \leq 72000 \Rightarrow 3x + y \leq 600 \dots (i)$$

$$x + y \leq 300 \dots (ii)$$

$$x + 100 \geq y \Rightarrow y \leq x + 100 \dots (iii)$$

$$\text{Profit: } Z = 200x + 120y$$

Therefore, the required LPP to maximize the profit is

Maximize $Z = 200x + 120y$ subject to constraints

$$3x + y \leq 600, x + y \leq 300, y \leq x + 100, x \geq 0, y \geq 0.$$