

## Exemplar Problems

### Linear Programming

13. A company manufactures two types of screws A and B. All the screws have to pass through a threading machine and a slotting machine. A box of Type A screws requires 2 minutes on the threading machine and 3 minutes on the slotting machine. A box of type B screws requires 8 minutes of threading on the threading machine and 2 minutes on the slotting machine. In a week, each machine is available for 60 hours.

On selling these screws, the company gets a profit of Rs 100 per box on type A screws and Rs 170 per box on type B screws.

Formulate this problem as a LPP given that the objective is to maximize profit.

**Solution:**

Let's consider that the company manufactures  $x$  boxes of type A screws and  $y$  boxes of type B screws.

From the given information the below table is constructed:

Items	Type A (x)	Type B (y)	Minimum time available on each machine in a week
Time required on threading machine	2	8	$60 \times 60 = 3600$ minutes
Time required on slotting machine	3	2	$60 \times 60 = 3600$ minutes
Profit	Rs 100	Rs 170	

From the data in the above table, the objective function for maximum profit  $Z = 100x + 170y$

Subject to the constraints

$$2x + 8y \leq 3600 \Rightarrow x + 4y \leq 1800 \dots (i)$$

$$3x + 2y \leq 3600 \dots (ii)$$

$$x \geq 0, y \geq 0 \text{ (non-negative constraints)}$$

Therefore, the required LPP is

$$\text{Maximize: } Z = 100x + 170y$$

Subject to constraints,

$$x + 4y \leq 1800, 3x + 2y \leq 3600, x \geq 0, y \geq 0.$$