

PERMUTATIONS AND COMBINATIONS - Class XI

Related Questions with Solutions

Questions

Question: 01

For some natural N , the number of positive integral 'x' satisfying the equation,
 $1! + 2! + 3! + \dots + (x!) = (N)^2$ is :

- A. none
- B. one
- C. two
- D. infinite

Solutions

Solution: 01

$$1! + 2! + 3! + 4! + 5! + \dots + x! = N^2$$

$$1 + 2 + 6 + 24 + 120 + \dots = N^2$$

For $x!$ when $x \geq 5$, unit digit is zero

$1 + 2 + 6 + 24 = 33$, unit digit is 3

so, for $x \geq 5$, unit digit of sum on L.H.S. will be 3

so, it can't be a perfect square.

No, for $x = 3$ $1 + 2 + 6 = 9$

for $x = 1$ $1! = 1$

\therefore Two perfect squares are obtained.

\therefore Two positive integral 'x' is obtained.

Correct Options

Answer:01

Correct Options: C