

Exemplar Problems

Permutation and Combination

5. We wish to select 6 persons from 8, but if the person A is chosen, then B must be chosen. In how many ways can selections be made?

Solution:

We know that,

$${}^n C_r = \frac{n!}{r!(n-r)!}$$

According to the question,

Case 1:

If both A and B are selected = $1 \times 1 \times {}^6 C_4$

$$= \frac{6!}{4!(6-4)!} = \frac{6!}{4!2!} = 15$$

Case 2:

If neither A nor B are selected = ${}^6 C_6 = 1$

If B is selected but A is not selected = $1 \times {}^6 C_5$

$$= \frac{6!}{5!(6-4)!} = 6$$

Adding the results of both A and B being selected, neither A nor B being selected and B being selected but A not being selected,

We get,

$$15+1+6=22$$