

Question 4: The equation of the plane passing through the point (1, 1, 1) and perpendicular to the planes $2x + y - 2z = 5$ and $3x - 6y - 2z = 7$ is

(a) $14x+2y+15z = 31$

(b) $14x+2y-15z = 1$

(c) $-14x+2y+15z = 3$

(d) $14x-2y+15z = 27$

Solution:

Let plane $P_1 \Rightarrow 2x + y - 2z = 5$

$P_2 \Rightarrow 3x - 6y - 2z = 7$

Let P be the plane perpendicular to P_1 and P_2

Also P passes through (1, 1, 1).

Hence required equation =

$$\begin{vmatrix} x-1 & y-1 & z-1 \\ 2 & 1 & -2 \\ 3 & -6 & -2 \end{vmatrix} = 0$$

$$\Rightarrow (x-1)(-2-12) - (y-1)(-4+6) + (z-1)(-12-3) = 0$$

$$\Rightarrow 14x-14+2y-2+15z-15 = 0$$

$$\Rightarrow 14x + 2y + 15z = 31$$

Hence option a is the answer.