

Q 3.

A particle of mass m is initially at rest at the origin. It is subjected to a force and starts moving along the x -axis. Its kinetic energy K changes with time as $dK/dt = \gamma t$, where γ is a positive constant of appropriate dimensions. Which of the following statements is (are) true?

- A The force applied on the particle is constant
- B The speed of the particle is proportional to time
- C The distance of the particle from the origin increases linearly with time
- D The force is conservative

Solution:

$$\frac{dk}{dt} = \gamma t \text{ and } k = \frac{1}{2}mv^2$$

Differentiating $k = \frac{1}{2}mv^2$ w.r.t. time

$$\therefore \frac{dk}{dt} = mv \frac{dv}{dt} = \gamma t$$

$$\therefore m \int_0^v v dv = \gamma \int_0^t t dt$$

$$\frac{mv^2}{2} = \frac{\gamma t^2}{2}$$

$$v = \sqrt{\frac{\gamma}{m}} t$$

$\Rightarrow v \propto t$; So option (B) is correct

since $F = ma$

$$\text{And } a = \frac{dv}{dt} = \sqrt{\frac{\gamma}{m}}$$

$$\therefore F = m \sqrt{\frac{\gamma}{m}} = \sqrt{\gamma m} = \text{constant}$$

Here resultant force which is applied force in this case is constant.

So option (A) is correct

Since force applied is constant and displacement between any two points on x -axis will also be constant, thus work done will be independent of path, hence force is conservative in nature, So option D is correct

Option (A), (B) and (D) are correct answers