Prove that the maximum horizontal range is four times the maximum height attained by the projectile; when fired at an inclination so as to have maximum horizontal range.

Solution For $\theta = 45^{\circ}$, the horizontal range is maximum and is given by

$$R_{\text{max}} = \frac{u^2}{g}$$

$$H_{\text{max}} = \frac{u^2 \sin^2 45^\circ}{2g} = \frac{u^2}{4g} = \frac{R_{\text{max}}}{4}$$

Maximum height attained

or

$$R_{\text{max}} = 4 H_{\text{max}}$$

Proved.