

QUES 03:-

Following are four different relations about displacement, velocity and acceleration for the motion of a particle in general. Choose the incorrect one (s) :

i. $v_{av} = \frac{1}{2} [v(t_1) + v(t_2)]$

ii. $v_{av} = \frac{r(t_2) - r(t_1)}{t_2 - t_1}$

iii. $r = \frac{1}{2} (v(t_2) - v(t_1))(t_2 - t_1)$

iv. $a_{av} = \frac{v(t_2) - v(t_1)}{t_2 - t_1}$

Sol. (a, c) When an object covers a displacement Δr in time Δt , its average velocity is given by

$$\vec{v}_{avg} = \frac{\vec{\Delta r}}{\Delta t} = \frac{r_2 - r_1}{t_2 - t_1} \text{ where } r_1 \text{ and } r_2 \text{ are position vectors corresponding to time } t_1 \text{ and } t_2$$

If the velocity of an object changes from v_1 to v_2 in time Δt , the average acceleration is given by

$$a_{av} = \frac{\Delta v}{\Delta t} = \frac{v_2 - v_1}{t_2 - t_1}$$

But, when acceleration is non-uniform,

$$v_{av} \neq \frac{v_1 + v_2}{2}$$

Option (c) is similar to the relation $\vec{r} = \frac{1}{2} at^2$ which is not correct if initial velocity is given.

So (b) and (d) are the correct relations for the uniform acceleration.