

1. A cylinder with a movable piston contains 3 moles of hydrogen at standard temperature and pressure. The walls of the cylinder are made of a heat insulator, and the piston is insulated by having a pile of sand on it. By what factor does the pressure of the gas increase if the gas is compressed to half its original volume?

Sol. Here the process is adiabatic compression and $V_2 = \frac{V_1}{2}$, $P_1 = 1 \text{ atm}$ and for hydrogen (a diatomic gas) $\gamma = 1.4$.

$$\therefore P_1 V_1^\gamma = P_2 V_2^\gamma$$

$$\text{Hence } P_2 = P_1 \left(\frac{V_1}{V_2} \right)^\gamma = 1 \text{ atm} \left(\frac{V_1}{\frac{V_1}{2}} \right)^{1.4}$$

$$\Rightarrow P_2 = (2)^{1.4} \text{ atm}$$

$$= 2.64 \text{ atm}$$