

Binomial Theorem - Class XI

Related Questions with Solutions

Questions

Question: 01

In questions below, If $C_0, C_1, C_2, \dots, C_n$ are the combinatorial coefficients in the expansion of $(1 + x)^n$, $n \in \mathbb{N}$, then

$$C_0^2 + C_1^2 + C_2^2 + \dots + C_n^2 =$$

- A. ${}^{2n}C_n$
- B. ${}^{2n}C_{n-1}$
- C. $({}^{2n}C_n)^2$
- D. $({}^{2n}C_{n-1})^2$

Solutions

Solution: 01

$$[1 + x]^n = {}^nC_0 + {}^nC_1x + {}^nC_2x^2 + \dots + {}^nC_nx^n$$

$$[x + 1]^n = {}^nC_0x^n + {}^nC_1x^{n-1} + \dots + {}^nC_n$$

multiply

$$[1 + x]^{2n} = [{}^nC_0 + {}^nC_1x + \dots + {}^nC_nx^n] [{}^nC_0x^n + \dots + {}^nC_n]$$

$${}^nC_0^2 + {}^nC_1^2 + \dots + {}^nC_n^2 = \text{coefficient of } x^n \text{ in } (1 + x)^{2n}$$

$$= {}^{2n}C_n$$

Correct Options

Answer:01

Correct Options: A