

5. Prove that the mid-point of the hypotenuse of a right-angled triangle is equidistant from its vertices.

Solution Here, $\angle CAB = 90^\circ$, let D be the mid-point of the hypotenuse BC .

$$BD = DC$$

$$AB = AD + DB$$

$$AC = AD + DC = AD + BD$$

Since, $\angle BAC = 90^\circ$ $AB \perp AC$

$$(AD + DB) \cdot (AD + BD)$$

$$(AD - BD) \cdot (AD + BD)$$

$$AD^2 - BD^2$$

$$AD = BD \text{ also } BD = DC$$

\therefore

$\therefore D$ is mid-point of BC

Thus, $|AD| = |BD| = |DC|$. Hence, the result.