

Q.02

(a) Three resistors $2\ \Omega$, $4\ \Omega$ and $5\ \Omega$ are combined in parallel. What is the total resistance of the combination?

(b) If the combination is connected to a battery of emf $20\ \text{V}$ and negligible internal resistance, determine the current through each resistor, and the total current drawn from the battery.

Answer

(a) There are three resistors of resistances,

$$R_1 = 2\ \Omega, R_2 = 4\ \Omega, \text{ and } R_3 = 5\ \Omega$$

They are connected in parallel. Hence, total resistance (R) of the combination is given by,

$$\begin{aligned}\frac{1}{R} &= \frac{1}{R_1} + \frac{1}{R_2} + \frac{1}{R_3} \\ &= \frac{1}{2} + \frac{1}{4} + \frac{1}{5} = \frac{10+5+4}{20} = \frac{19}{20} \\ \therefore R &= \frac{20}{19}\ \Omega\end{aligned}$$

Therefore, total resistance of the combination is $\frac{20}{19}\ \Omega$.

(b) Emf of the battery, $V = 20 \text{ V}$

Current (I_1) flowing through resistor R_1 is given by,

$$\begin{aligned} I_1 &= \frac{V}{R_1} \\ &= \frac{20}{2} = 10 \text{ A} \end{aligned}$$

Current (I_2) flowing through resistor R_2 is given by,

$$\begin{aligned} I_2 &= \frac{V}{R_2} \\ &= \frac{20}{4} = 5 \text{ A} \end{aligned}$$

Current (I_3) flowing through resistor R_3 is given by,

$$\begin{aligned} I_3 &= \frac{V}{R_3} \\ &= \frac{20}{5} = 4 \text{ A} \end{aligned}$$

Total current, $I = I_1 + I_2 + I_3 = 10 + 5 + 4 = 19 \text{ A}$

Therefore, the current through each resistor is 10 A, 5 A, and 4 A respectively and the total current is 19 A.