

Q.05 Work done by a force \mathbf{F} on a body is $W = \mathbf{F} \cdot \mathbf{s}$, where \mathbf{s} is the displacement of body. Given that under a force \mathbf{F} a body is displaced from position vector $\mathbf{r}_1 = (2\hat{\mathbf{i}} + 3\hat{\mathbf{j}} + 4\hat{\mathbf{k}}) \text{ m}$ to $\mathbf{r}_2 = (\hat{\mathbf{i}} + \hat{\mathbf{j}} + \hat{\mathbf{k}}) \text{ m}$. Find the work done by this force.

Solution The body is displaced from \mathbf{r}_1 to \mathbf{r}_2 . Therefore

$$\mathbf{s} = \mathbf{r}_2 - \mathbf{r}_1 = (\hat{\mathbf{i}} + \hat{\mathbf{j}} + \hat{\mathbf{k}}) - (2\hat{\mathbf{i}} + 3\hat{\mathbf{j}} + 4\hat{\mathbf{k}})$$

Now, work done by the force is $W = \mathbf{F} \cdot \mathbf{s}$

$$= (2\hat{\mathbf{i}} + 3\hat{\mathbf{j}} + 4\hat{\mathbf{k}}) \cdot (-\hat{\mathbf{i}} - 2\hat{\mathbf{j}} - 3\hat{\mathbf{k}})$$

$$= (2)(-1) + (3)(-2) + (4)(-3)$$