

Vectors - Class XII

Related Questions with Solutions

Questions

Question: 01

If $\vec{a} = \hat{i} + \hat{j} + \hat{k}$, $\vec{b} = 4\hat{i} + 3\hat{j} + 4\hat{k}$ and $\vec{c} = \hat{i} + \alpha\hat{j} + \beta\hat{k}$ are linearly dependent vectors & $|\vec{c}| = \sqrt{3}$, then

- A. $\alpha = 1, \beta = -1$
- B. $\alpha = 1, \beta = \pm 1$
- C. $\alpha = -1, \beta = \pm 1$
- D. $\alpha = \pm 1, \beta = 1$

Solutions

Solution: 01

$$\vec{c} = \hat{i} + \alpha\hat{j} + \beta\hat{k}$$

$$|\vec{c}| = \sqrt{3}$$

$$1 + \alpha^2 + \beta^2 = 3 \Rightarrow \alpha^2 + \beta^2 = 2$$

$$\begin{vmatrix} 1 & 1 & 1 \\ 4 & 3 & 4 \\ 1 & \alpha & \beta \end{vmatrix} = 0$$

$$3\beta - 4\alpha - 4\beta + 4 + 4\alpha - 3 = 0$$

$$-\beta + 1 = 0$$

$$\beta = 1$$

$$\alpha^2 + 1 = 2$$

$$\alpha = \pm 1$$

Correct Options

Answer:01

Correct Options: D