

If $a, b, c \in \mathbb{Q}$,

1) D is a square $\Rightarrow \alpha, \beta \in \mathbb{Q}$

2) D is not a square $\Rightarrow \alpha, \beta$ are conjugate surds

$a, b, c \in \mathbb{R}, a > 0$

1) If $D > 0$, then α, β are distinct and real

2) If $D = 0$, then $\alpha = \beta$, are real

3) If $D < 0$, then α, β are distinct and complex conjugates of each other

$$ax^2 + bx + c = 0 \quad a, b, c \in \mathbb{C}$$

$$1) \quad \alpha + \beta = \frac{-b}{2a} + \left(\frac{-b}{2a}\right) = \frac{-b}{a}$$

$$2) \quad \alpha\beta = \left(\frac{-b}{2a}\right)^2 - \left(\frac{\sqrt{b^2 - 4ac}}{2a}\right)^2 = \frac{c}{a}$$

$$3) \quad |\alpha - \beta| = \left| \frac{\sqrt{b^2 - 4ac}}{a} \right|$$

$$4) \quad a\alpha^2 + b\alpha + c = 0$$

$$a\beta^2 + b\beta + c = 0$$