

Derivative - Class XII

Related Questions with Solutions

Questions

Question: 01

Let $f(x) = x + \sin x$. Suppose g denotes the inverse function of f . The value of $g' \left(\frac{\pi}{4} + \frac{1}{\sqrt{2}} \right)$ has the value equal to

- A. $\sqrt{2} - 1$
- B. $\frac{\sqrt{2} + 1}{\sqrt{2}}$
- C. $2 - \sqrt{2}$
- D. $\sqrt{2} + 1$

Solutions

Solution: 01

$$f(x) = y = x + \sin x$$

$$\frac{dy}{dx} = 1 + \cos x \quad \text{where } y = \frac{\pi}{4} + \frac{1}{\sqrt{2}} = x + \sin x \Rightarrow x = \frac{\pi}{4}$$

$$g'(y) = \frac{dx}{dy} = \frac{1}{1 + \cos x}$$

$$\therefore g' \left(\frac{\pi}{4} + \frac{1}{\sqrt{2}} \right) = \frac{1}{1 + (1/\sqrt{2})} = \frac{\sqrt{2}}{\sqrt{2} + 1} = \sqrt{2}(\sqrt{2} - 1) = 2 - \sqrt{2}$$

Correct Options

Answer:01

Correct Options: C