

DERIVATIVE OF STANDARD FUNCTIONS

$f(x)$	$\frac{d}{dx}(f(x))$	$f(x)$	$\frac{d}{dx}(f(x))$
x^n	$nx^{n-1}; n \in \mathbb{R}$	$\sec x$	$\sec x \tan x, x \neq (2n+1)\frac{\pi}{2}$
e^x	e^x	$\operatorname{cosec} x$	$-\operatorname{cosec} x \cot x; x \neq n\pi$
x^x	$x^x(1 + \ln x)$	$\cot x$	$-\operatorname{cosec}^2 x, x \neq n\pi$
a^x	$a^x \log_e a; a > 0, a \neq 1$	$\sin^{-1} x$	$\frac{1}{\sqrt{1-x^2}}; -1 < x < 1$
$\log_e x$	$\frac{1}{x}; x > 0$	$\cos^{-1} x$	$-\frac{1}{\sqrt{1-x^2}}; -1 < x < 1$
$\log_a x$	$\frac{1}{x \log_e a}; x > 0$	$\tan^{-1} x$	$\frac{1}{1+x^2}; x \in \mathbb{R}$
$\sin x$	$\cos x$	$\sec^{-1} x$	$\frac{1}{ x \sqrt{x^2-1}}; x > 1$
$\cos x$	$-\sin x$	$\operatorname{cosec}^{-1} x$	$\frac{-1}{ x \sqrt{x^2-1}}; x > 1$
$\tan x$	$\sec^2 x; x \neq (2n+1)\frac{\pi}{2}, n \in \mathbb{I}$	$\cot^{-1} x$	$\frac{-1}{1+x^2}; x \in \mathbb{R}$

RULES FOR DIFFERENTIATION

$$\frac{d}{dx}(K(f(x))) = K \cdot \frac{d}{dx}(f(x)), \text{ where } K \text{ is constant}$$

$$\frac{d}{dx}\{f(x) \pm g(x)\} = \frac{d}{dx}(f(x)) \pm \frac{d}{dx}(g(x))$$

$$\text{Product Rule: } \frac{d}{dx}\{f(x) \cdot g(x)\} = f(x) \frac{d}{dx}(g(x)) + g(x) \frac{d}{dx}(f(x))$$

$$\text{Quotient Rule: } \frac{d}{dx} \left\{ \frac{f(x)}{g(x)} \right\} = \frac{g(x) \frac{d}{dx}(f(x)) - f(x) \frac{d}{dx}(g(x))}{(g(x))^2}$$

Chain Rule: If y is a function of u , u is a function of v and v a function of x , then

$$\frac{dy}{dx} = \frac{dy}{du} \times \frac{du}{dv} \times \frac{dv}{dx}$$

Parametric differentiation: If $x = P(t)$, $y = Q(t)$, where 't' is parameter then,

$$\frac{dy}{dx} = \frac{\frac{dy}{dt}}{\frac{dx}{dt}} = \frac{\frac{d}{dt}(Q(t))}{\frac{d}{dt}(P(t))} = \frac{Q'(t)}{P'(t)}$$

Differentiation of one function w.r.t. other function

$$\frac{d(f(x))}{d(g(x))} = \frac{\frac{d}{dx}(f(x))}{\frac{d}{dx}(g(x))} = \frac{f'(x)}{g'(x)}$$

Logarithmic differentiation: It is applicable in following cases:

All are functions of 'x'

$$\rightarrow y = \underbrace{f_1 \cdot f_2 \cdot f_3 \dots f_n}_{\text{(product, divide or power form)}}$$

$$\rightarrow y = (f(x))^{g(x)}$$

* Take log on both sides and then differentiate.