

Derivative - Class XII

Past Year JEE Questions

Questions

Question: 01

If g is the inverse of a function f and $f'(x) = \frac{1}{1+x^5}$ then $g'(x)$ is equal to:

- A. $\frac{1}{1+\{g(x)\}}$
- B. $1 + \{g(x)\}^5$
- C. $1 + x^5$
- D. $5x^4$

Solutions

Solution: 01

Explanation

Since $f(x)$ and $g(x)$ are inverse of each other

$$\therefore g'(f(x)) = \frac{1}{f'(x)}$$

$$\Rightarrow g'(f(x)) = 1 + x^5$$

$$\left(\text{As } f'(x) = \frac{1}{1+x^5} \right)$$

Here $x = g(y)$

$$\therefore g'(y) = 1 + \{g(y)\}^5$$

$$\Rightarrow g'(x) = 1 + \{g(x)\}^5$$