

Derivative - Class XII

Past Year JEE Questions

Questions

Question: 01

Let $f : (-1, 1) \rightarrow \mathbb{R}$ be a differentiable function with $f(0) = -1$ and $f'(0) = 1$. Let $g(x) = [f(2f(x) + 2)]^2$. Then $g'(0) =$

- A. -4
- B. 0
- C. -2
- D. 4

Solutions

Solution: 01

Explanation

$$g'(x) = 2(f(2f(x) + 2))$$

$$\left(\frac{d}{dx}(f(2f(x) + 2))\right)$$

$$= 2f(2f(x) + 2)f'(2f(x))$$

$$+ 2 \cdot (2f'(x))$$

$$\Rightarrow g'(0) = 2f(2f(0) + 2) \cdot$$

$$f'(2f(0) + 2) + 2f'(0)$$

$$= 4f(0)(f'(0))^2$$

$$= 4(-1)(1)^2 = -4$$