

4. Let $p, q \in \mathbb{R}$. If $2-\sqrt{3}$ is a root of the quadratic equations,

$x^2 + px + q = 0$, then:

(a) $p^2 - 4q + 12 = 0$

(b) $q^2 - 4p - 16 = 0$

(c) $q^2 + 4p + 14 = 0$

(d) $p^2 - 4q - 12 = 0$

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Solution: (d)

Since $2-\sqrt{3}$ is a root of the quadratic equation $x^2 + px + q = 0$
 $\therefore 2+\sqrt{3}$ is the other root.

$$\begin{aligned} \Rightarrow x^2 + px + q &= [x - (2 - \sqrt{3})] \cdot [x - (2 + \sqrt{3})] \\ &= x^2 - (2 + \sqrt{3})x - (2 - \sqrt{3})x + (2^2 - (\sqrt{3})^2) \\ &= x^2 - 4x + 1 \end{aligned}$$

Now, by comparing $p = -4$, $q = 1$.

$$\Rightarrow p^2 - 4q - 12 = 16 - 4 - 12 = 0.$$