

PROBLEM

In $[0, 1]$ Lagranges Mean Value theorem is NOT applicable to **(2003S)**

$$(a) \quad f(x) = \begin{cases} \frac{1}{2} - x & x < \frac{1}{2} \\ \left(\frac{1}{2} - x\right)^2 & x \geq \frac{1}{2} \end{cases}$$

$$(b) \quad f(x) = \begin{cases} \frac{\sin x}{x}, & x \neq 0 \\ 1, & x = 0 \end{cases}$$

$$(c) \quad f(x) = x|x|$$

$$(d) \quad f(x) = |x|$$

SOLUTION

(a) There is only one function in option (a) whose critical point $\frac{1}{2} \in (0, 1)$ for the rest of the parts critical point