JEE Advanced/ IIT-JEE

MCQs with One Correct Answer

PROBLEM

$$\frac{d^2x}{dv^2}$$
 equals

(2007 - 3 marks)

(a)
$$\left(\frac{d^2y}{dx^2}\right)^{-1}$$

(b)
$$-\left(\frac{d^2y}{dx^2}\right)^{-1}\left(\frac{dy}{dx}\right)^{-3}$$

(c)
$$\left(\frac{d^2y}{dx^2}\right)\left(\frac{dy}{dx}\right)^{-2}$$

(d)
$$-\left(\frac{d^2y}{dx^2}\right)\left(\frac{dy}{dx}\right)^{-3}$$

(d)
$$\frac{d^2x}{d^2y} = \frac{d}{dy} \left(\frac{dx}{dy} \right) = \frac{d}{dx} \left(\frac{dx}{dy} \right) \times \frac{dx}{dy}$$

$$= \left\{ \frac{d}{dx} \left[\frac{1}{\left(\frac{dy}{dx} \right)} \right] \right\} \times \frac{1}{\frac{dy}{dx}} = -\frac{1}{\left(\frac{dy}{dx} \right)^2} \times \frac{d^2y}{dx^2} \times \frac{1}{\left(\frac{dy}{dx} \right)}$$

$$= -\left(\frac{dy}{dx}\right)^{-3} \frac{d^2y}{dx^2}$$