

Q.1) If two angles of a triangle are  $\tan^{-1}(2)$  &  $\tan^{-1}(3)$ , then find the third angle.

Soln- Two angles are  $\tan^{-1}(2)$  &  $\tan^{-1}3$ .

Sum of all angles of a triangle is  $\pi$ .  
So, the third angle will be  $\pi - \tan^{-1}(2) - \tan^{-1}(3)$

$$\begin{aligned}\pi - \tan^{-1}(2) - \tan^{-1}(3) &= \pi - (\tan^{-1}(2) + \tan^{-1}(3)) \\ &= \pi - \left[ \pi + \tan^{-1}\left(\frac{2+3}{1-2\cdot3}\right) \right] \quad \text{as } (2)(3) > 1 \\ &= -\tan^{-1}\left(\frac{5}{-5}\right) \\ &= -\tan^{-1}(-1) \\ &= -\left(-\frac{\pi}{4}\right) = \frac{\pi}{4}\end{aligned}$$

hence, the third angle of triangle is  $\frac{\pi}{4}$ .