

1. To reduce power of functions  $\int \tan^n x dx, \int \cot^n x dx, \int \sec^n x dx, \int \operatorname{cosec}^n x dx$

(a) If  $I_n = \int \tan^n x dx$ , then  $I_n = \frac{\tan^{n-1} x}{n-1} - I_{n-2}$

(b) If  $I_n = \int \cot^n x dx$ , then  $I_n = -\frac{\cot^{n-1} x}{n-1} - I_{n-2}$

(c) If  $I_n = \int \sec^n x dx$ , then  $I_n = \frac{\tan x \sec^{n-2} x}{n-1} + \frac{n-2}{n-1} I_{n-2}$

(iv) If  $I_n = \int \operatorname{cosec}^n x$ , then  $I_n = \frac{\cot x \operatorname{cosec}^{n-2} x}{n-1} + \frac{n-2}{n-1} I_{n-2}$

2. Integration of type  $\int \sin mx \cdot \cos nx dx$

a) If  $m$  and  $n$  are even natural numbers then express  $\sin mx \cos nx$  in the terms of sines and cosines of multiples of  $x$  by using trigonometric results or De' Moivre's theorem.

b) If  $m$  is an odd number then put  $\cos x = t$ .

If  $n$  is an odd number then put  $\sin x = t$ .

If both  $m$  and  $n$  are odd numbers then put either  $\sin x = t$  or  $\cos x = t$ .

c) When  $m + n$  is a negative even integer then put  $\tan x = t$ .