

A gas bubble, from an explosion under water, oscillates with a period  $T$  proportional to  $p^a d^b E^c$ . Where ' $P$ ' is the static pressure, ' $d$ ' is the density of water and ' $E$ ' is the total energy of the explosion. Find the values of  $a$ ,  $b$  and  $c$ .

As per question,  $T \propto P^a d^b E^c$  or  $[T] = [P]^a [d]^b [E]^c$

or  $[M^0 L^0 T^1] = [ML^{-1} T^{-2}]^a [ML^{-3}]^b [ML^2 T^{-2}]^c$

or  $M^0 L^0 T^1 = M^{a+b+c} L^{-a-3b+2c} T^{-2a-2c}$

$$\therefore a + b + c = 0 \quad \dots (i)$$

$$-a - 3b + 2c = 0 \quad \dots (ii)$$

$$-2a - 2c = 1 \quad \dots (iii)$$

Solving, eqns. (i), (ii) and (iii) we get

$$a = -5/6, b = 1/2, c = 1/3.$$