

$$P(A|B) = \frac{P(A \cap B)}{P(B)}$$

Multiplication rule: $P(A \cap B) = P(A|B) P(B)$
 $= P(B|A) P(A)$

For n events: $P\left(\bigcap_{i=1}^n A_i\right) = P(A_1) \cdot P(A_2|A_1) \cdot P(A_3|A_1, A_2)$
 $\dots \cdot P(A_n | \bigcap_{i=1}^{n-1} A_i)$

• Total probability theorem:

$$P(A) = P(A|B_1) P(B_1) + P(A|B_2) P(B_2) + \dots$$

$$+ P(A|B_n) P(B_n)$$

• Bayes Theorem:

$$P(B_r|A) = \frac{P(A|B_r) P(B_r)}{\sum_{i=1}^n P(A|B_i) P(B_i)} \quad r=1, 2, \dots, n$$

• Two independent events: $P(A \cap B) = P(A) \cdot P(B)$

• Three independent events: $P(A \cap B) = P(A) P(B)$

$$P(B \cap C) = P(B) P(C)$$

$$P(A \cap C) = P(A) P(C)$$

$$P(A \cap B \cap C) = P(A) P(B) P(C)$$