

Q. A series R-C combination is connected to an AC voltage of angular frequency $\omega = 500$ radian/s. If the impedance of the R-C circuit is $R\sqrt{1.25}$, the time constant (in millisecond) of the circuit is ?

3. In given R-C circuit,

$$\omega = 500 \text{ rad/s}; \quad Z = R\sqrt{1.25}$$

$$\Rightarrow Z^2 = R^2(1.25)$$

$$\Rightarrow \frac{1}{(\omega C)^2} + R^2 = R^2(1.25)$$

$$\Rightarrow \frac{1}{(\omega C)^2} = (0.25)R^2$$

$$\Rightarrow \left(\frac{1}{\omega C}\right)^2 = (0.5R)^2$$

$$\Rightarrow \frac{1}{\omega C} = \left(\frac{1}{2}\right)R$$

$$\Rightarrow \frac{2}{\omega} = RC$$

$$\Rightarrow \frac{2}{500} = \tau \left\{ \begin{array}{l} \because \tau = RC \text{ is the} \\ \text{time constant of} \\ \text{R-C circuit} \end{array} \right\}$$

$$\Rightarrow 4 \times 10^{-4} \text{ s} = \tau$$

$$\Rightarrow \boxed{\tau = 4 \text{ ms}}$$