

If the expression in powers of  $x$  of the function  $\frac{1}{[1-ax][1-bx]}$  is  $q_0 + a_1x + a_2x^2 + \dots$

then  $a_n$  is?

$$(1-ax)^{-1} (1-bx)^{-1} = (1+ax+a^2x^2+\dots) (1+bx+b^2x^2+\dots)$$

Coeff. of  $x^n$  is  $\{ b^n + ab^{n-1} + a^2b^{n-2} + \dots + a^{n-1}b + a^n \}$ .

$$\Rightarrow \frac{b^{n+1} - a^{n+1}}{b-a}$$

$$\Rightarrow a_n = \frac{b^{n+1} - a^{n+1}}{b-a}$$

$$[a^p - b^p = (a-b)(a^{p-1}b^1 + a^{p-2}b^2 + a^{p-3}b^3 \dots + a^1b^{p-1})] p \in \mathbb{N}$$

**NOTE** : the above formula will be discussed in the future so try to remember this formula