

Que5:

An investigator interviewed 100 students to determine their preferences for the three drinks : milk (M), coffee (C) and tea (T). He reported the following : 10 students had all the three drinks M , C and T ; 20 had M and C ; 30 had C and T ; 25 had M and T ; 12 had M only; 5

had C only; and 8 had T only. Using a Venn diagram find how many did not take any of the three drinks.

Ans:

$n(U) = 100$, where U stands for universal set

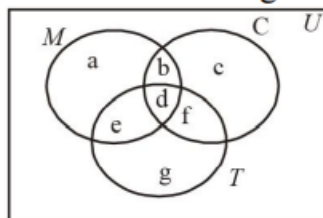
$n(M \cap C \cap T) = d = 10$; $n(M \cap C) = b + d = 20$;

$n(C \cap T) = d + f = 30$; $n(M \cap T) = d + e = 25$;

$\Rightarrow b = 10, f = 20$ and $e = 15$

$n(\text{only } M) = a = 12$; $n(\text{only } C) = c = 5$; $n(\text{only } T) = g = 8$

Filling all the entries we obtain the Venn diagram as shown :



$$\begin{aligned} \therefore n(M \cap C \cup T) &= a + b + c + d + e + f + g \\ &= 12 + 10 + 5 + 15 + 10 + 20 + 8 = 80 \end{aligned}$$

$$\therefore n(M \cup C \cup T)' = 100 - 80 = 20$$