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SET: A set is a collection of well defined objects which are distinct from each other.

Sets are generally denoted by capital letters A, B, C and the elements of the set by a, b, c, \dots etc.

If a is an element of a set A , then write $a \in A$ and say a belongs to A .

SUBSETS :- Let A and B be two sets if every element of A is an element of B , then A is called a subset of B if A is subset of B . We write $A \subseteq B$.

Example

$$A = \{1, 2, 3, 4\}$$

$$B = \{1, 2, 3, 4, 5, 6, 7\}$$

$$\Rightarrow \boxed{A \subseteq B}$$

PROPER SUBSET :- If A is a subset of B and $A \neq B$, then A is a proper subset of B and we write $A \subset B$.

POWER SET :- Let A be any set. The set of all subsets of A is called power set of A and is denoted by $P(A)$. To calculate the total number of sets present in a power set we have to use the formula:
No of sets in $\boxed{P(A) = 2^n}$ n :- No of element in set A .

SOME OPERATIONS ON SETS

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- (i) Union of two set: $A \cup B = \{x : x \in A \text{ or } x \in B\}$
- (ii) Intersection of two set: $A \cap B = \{x : x \in A \text{ and } x \in B\}$
- (iii) De-Morgan Law: $(A \cup B)' = A' \cap B'$
 $(A \cap B)' = A' \cup B'$

if A and B are any two sets then

- (i) $A - B = A \cap B'$
- (ii) $B - A = B \cap A'$
- (iii) $A - B = A \Leftrightarrow A \cap B = \phi$
- (iv) $(A - B) \cup B = A \cup B$
- (v) $(A - B) \cap B = \phi$
- (vi) $(A - B) \cup (B - A) = (A \cup B) - (A \cap B)$

SOME IMPORTANT RESULTS ON NUMBER OF ELEMENT IN SETS

if A, B, and C are finite set, and U be the finite universal set, then

- ① $n(A \cup B) = n(A) + n(B) - n(A \cap B)$
- ② $n(A \cup B) = n(A) + n(B) \Leftrightarrow A, B$ are disjoint non-void set

$$(iii) \quad n(A-B) = n(A) - n(A \cap B) \quad \text{s.e}$$

$$n(A-B) + n(A \cap B) = n(A)$$

(iv) $n(A \Delta B)$ = No of elements which belongs to exactly one of A or B.

$$n(A \Delta B) = n(A-B) \cup (B-A)$$

$$= n(A-B) + n(B-A) \quad \left[\because (A-B) \text{ and } (B-A) \text{ are disjoint} \right]$$

$$n(A \Delta B) = n(A) + n(B) - 2n(A \cap B)$$

$$(v) \quad n(A \cup B \cup C) = n(A) + n(B) + n(C) - n(A \cap B) - n(B \cap C) - n(C \cap A) + n(A \cap B \cap C)$$

$$(vi) \quad n(A' \cup B') = n((A \cap B)') = n(U) - n(A \cap B)$$

$$(vii) \quad n(A' \cap B') = n((A \cup B)') = n(U) - n(A \cup B)$$