

Question: -

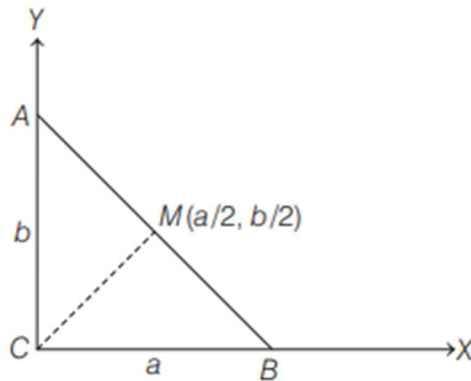
In a $\triangle ABC$, let $\angle C = \pi / 2$. If r is the inradius and R is the circumradius of the triangle, then $2(r + R)$ is equal to (2000, 2M)

- (a) $a + b$ (b) $b + c$ (c) $c + a$ (d) $a + b + c$

Solution: -

$$\text{Here, } R^2 = MC^2 = \frac{1}{4}(a^2 + b^2) \quad [\text{by distance from origin}]$$

$$= \frac{1}{4}c^2 \quad [\text{by Pythagoras theorem}]$$



$$\Rightarrow \quad R = \frac{c}{2}$$

$$\text{Next, } r = (s - c) \tan (C/2) = (s - c) \tan \pi / 4 = s - c$$

$$\begin{aligned} \therefore \quad 2(r + R) &= 2r + 2R = 2s - 2c + c \\ &= a + b + c - c \\ &= a + b \end{aligned}$$