# **Related Questions with Solutions**

### Questions

## **Ouetion: 01**

Consider the circles  $s_1: x^2+y^2=4$  and  $s_2: x^2+y^2-2x-4y+4=0$  Which of the following statements are correct?

A. Number of common tangents to these circles is 2.

B. If the power of a variable point P w.r.t. these two circles is same then P moves on the line x + 2y - 4 = 0.

C. Sum of the y-intercepts of both the circles is 6.

D. The circles  $S_1$  and  $S_2$  are orthogonal.

#### **Solutions**

# **Solution: 01**

$$\begin{array}{c} \overline{s_1:x^2+y^2=4} \text{ and } s_2=x^2+y^2-2x-4y+4=0\\ \text{centre:}\,(0,0); \text{radius}[r_1]=2; & \text{centre:}\,(1,2); \text{radius}[r_2]=1\\ \text{[A]}\,d=\text{distance between centres}=\sqrt{5}\\ r_1+r_2=3 & \Rightarrow |r_1-r_2|=1\\ \therefore |r_1-r_2| \leqslant d \leqslant r_1+r_2\\ \therefore \text{ these } 2 \text{ circles are intersecting.}\\ \therefore \text{ number of common tangents is } 2. \Rightarrow \text{[A] is correct}\\ \text{[B]}\,Let \quad P=(h,k)\\ \text{power of point } P \text{ is same w.r.t. these two circles.}\\ \therefore \sqrt{h^2+k^2-4}=\sqrt{h^2+k^2-2h-4k+4}\\ -4=-2h-4k+4\\ 2h+4k-8=0\\ x+2y-4=0\Rightarrow \text{[B]} \text{ is correct}\\ \text{[C] y intercept of } S_1 \text{ is } 2\sqrt{+4}=4\\ y \text{ intercept of } S_2 \text{ is } 2\sqrt{4-4}=0\\ \therefore \text{ sum of } y \text{ -intercept}=4\Rightarrow \text{[C] is incorrect}\\ \text{[D]}\,2(0+0)=-4+4\Rightarrow \text{[D] is correct]} \end{array}$$

## **Correct Options**

Answer:01

Correct Options: A, B, D