

$$\int \frac{1}{[(x-1)^3(x+2)^5]^{1/4}} dx.$$

$$\text{Answer: } I = \int \frac{1}{\left(\frac{x-1}{x+2}\right)^{3/4} (x+2)^2}$$

$$\text{Let } \frac{x-1}{x+2} = t \text{ or } \frac{3dx}{(x+2)^2} = dt$$

$$\therefore I = \frac{1}{3} \int \frac{1}{t^{3/4}} dt$$

$$= \frac{1}{3} \left(\frac{t^{1/4}}{1/4} \right) + C$$

$$= \frac{4}{3} t^{1/4} + C$$

$$= \frac{4}{3} \left(\frac{x-1}{x+2} \right)^{1/4} + C$$