

If x, y, z are positive integers then value of expression

$(x+y)(y+z)(z+x)$ is

(A) $= 8xyz$ (B) $\geq 8xyz$ (C) $< 8xyz$ (D) $= 4xyz$

SOLUTION :

$$AM \geq GM$$

$$\therefore x+y \geq 2\sqrt{xy} \quad \text{--- (1)}$$

$$y+z \geq 2\sqrt{yz} \quad \text{--- (2)}$$

$$z+x \geq 2\sqrt{zx} \quad \text{--- (3)}$$

Multiply (1), (2), (3)

$$(x+y)(y+z)(z+x) \geq 8xyz$$